



# **Air Vehicle Design**

**AOE 4065 – 4066**

## ***II. Air Vehicle Design Fundamentals***

**Course Module A8**

**Trade Studies**

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Blacksburg, VA**



### Overview of AVD Courses

#### I. Foundational Elements

- F1. Design: *An Engineering Discipline*
- F2. Systems and Systems Thinking
- F3. Basics of Systems Engineering
- F4. Decision Making with Ethics and Integrity

#### II. Air Vehicle Design Fundamentals

- A1. Purpose & Process

##### Conceptual Design

- A2. Understand the Problem
- A3. Solve the Problem
- A4. Initial Sizing: *Takeoff Weight Estimation*
- A5. Initial Sizing: *Wing Loading and Thrust Loading Estimation*
- A6. Cost Considerations
- A7. Concept to Configuration: *Key Considerations*
- A7A. Configuration Layout: *Drawings & Loft*

##### Conceptual & Preliminary Design

- A8. Trade Studies
- A9. Use of Software Tools
- A10. Preliminary Design: *Baseline Design Refinement & Validation*

#### III. Project Management Topics

- P1. Basics of Project Management and Project Planning
- P2. Project Organization
- P3. Roles & Responsibilities of Team Members
- P4. Project Execution: *Teamwork for Success*
- P5. Project Risk Management
- P6. Delivering Effective Oral Presentations
- P7. Writing Effective Design Reports

## **Disclaimer**

*Prof. Pradeep Raj, Aerospace and Ocean Engineering, Virginia Tech,  
collected and compiled the material contained herein from publicly  
available sources solely for educational purposes.*

*Although a good-faith attempt is made to cite all sources of material,  
we regret any inadvertent omissions.*

## **CRUCIALLY IMPORTANT**

***CMs only introduce key topics and highlight some important concepts and ideas...but without sufficient detail.***

***We must use lots of Reference Material\* to add the necessary details!***

***(\*see Appendix in the Overview CM)***



# Outline

## A8. Trade Studies

**A8.1 General Remarks**

**A8.2 Design (or Configuration) Trades**

**A8.3 Mission Trades**

**A8.4 Technology Trades**

**A8.5 Carpet Plot Technique**

# What is a Trade Study?

**Definition: A Trade Study is a decision-making method used to identify the best solution among a group of proposed solutions.**

- The Defense Acquisition Encyclopedia

- A trade study examines qualified solutions against criteria such as cost, schedule, performance, weight, system configuration, complexity, the use of Commercial Off-the-shelf (COTS), and many others.
- Trade Studies are performed throughout an acquisition program, from concept development through system design.
- Trade studies involve sequentially making small changes to the design parameters and comparing the results to the baseline values. For example, the 'best' pair of wing loading and thrust loading for the lightest weight aircraft is determined using a trade study that systematically varies a set of baseline values and determines the effect on aircraft weight (see Sect. A8.5)

# Why conduct trade studies?

To meet the goal of the Aircraft Design Team which is to

***“INTEGRATE all...geometrical and dimensional requirements, equipment, structural components...into a vehicle that is BALANCED with respect to flight in all phases of its flight envelope and ground operations...Satisfy the DESIRED requirements with the lightest weight (or least cost) vehicle.”***

***-- Nathan Kirschbaum***



***Trade Studies are key to achieving the design goals***

# Purpose of Trade Studies in Conceptual Design Phase

- We have made initial estimates of  $W_{TO}$ ,  $W/S$ ,  $T/W$
- We *assumed (or estimated)* values of several parameters,  $AR$ ,  $C_{D0}$ ,  $L/D$ ,  $C_{L_{max}}$ ,  $sfc$ ,  $V$ , *cruise altitude*, etc.

- Can we say that we have the *BEST (lightest weight) vehicle* that is *balanced* and *satisfies ALL customer requirements*?

*Trade Studies (aka Parametric Studies) are conducted to produce evidence to answer this question in the affirmative!*

## Bottom Line

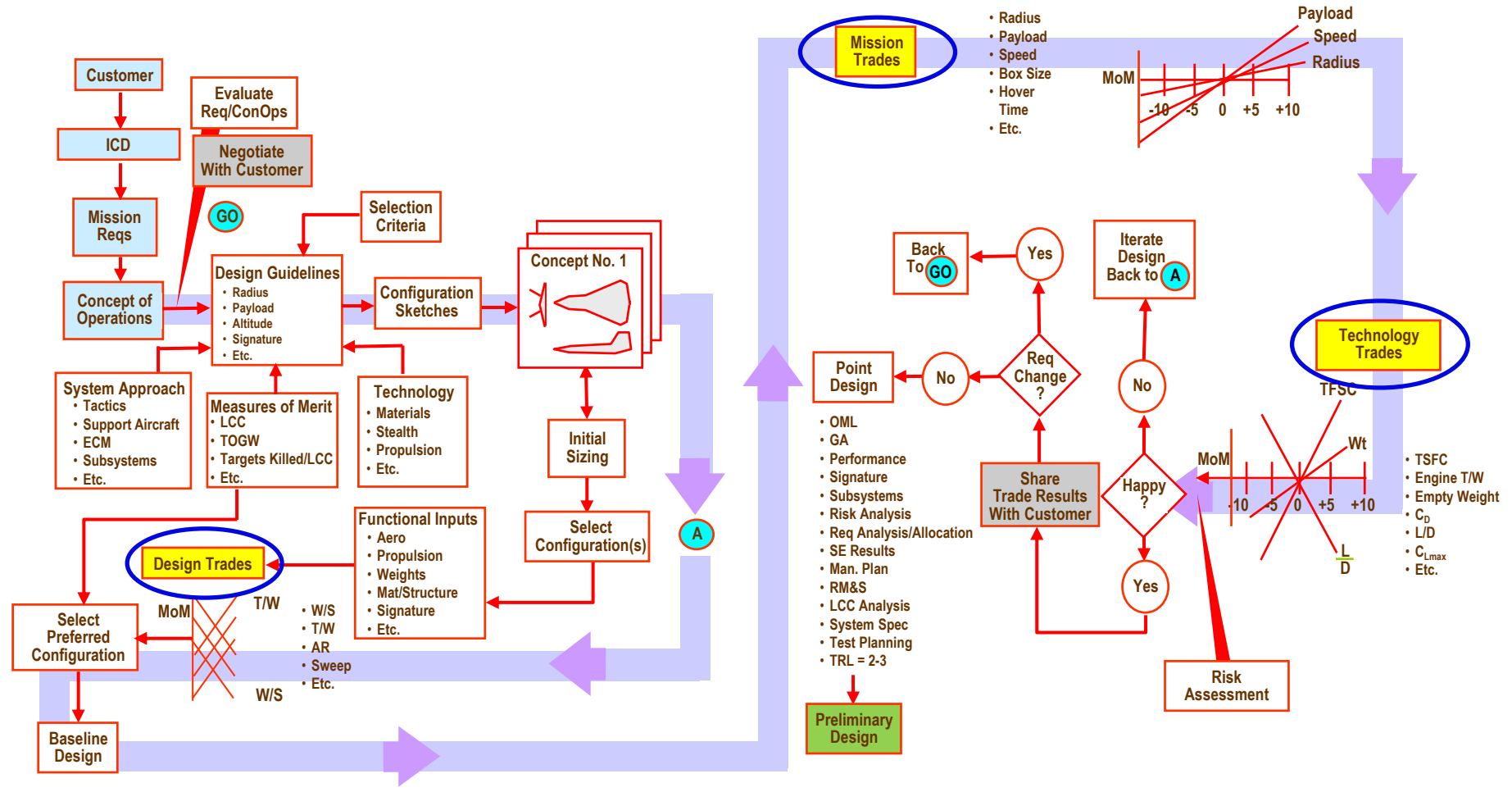
- Trade studies are pervasive in design
- The studies establish a basis for design decisions

**Caution:** Use Trade Study results in conceptual design as “indicators” or “flags,” not definitive answers—too early in the game!

**“Only through the trade studies will the true optimum aircraft emerge.” -- Raymer**



# Types of Trade Studies in Aircraft Conceptual Design



**Trade Studies help you select parameters for best design**

# Trade Studies Challenges

- ***Problem:*** Of a large number of parameters that affect aircraft design, *what combination of parameters will give the BEST design (lightest-weight aircraft or another Measure of Merit such as cost or fuel consumption) while meeting all requirements?*
- ***“Brute-force” Approach:*** Sort through all possible combinations of numerous parameters in a systematic manner to find the best set.
  - Easier said than done! Impractical to do by hand
  - Motivator for computer-assisted Multidisciplinary Design Optimization (MDO)
- **Performing parametric analyses is a tall order.**
- **Collecting and compiling all results for comparative evaluation to select the best combination is even more daunting.**
- **Visual display of Results (multi-dimensional data) that easily “convinces” the customer that you indeed have the best combination is priceless!**



# Example of Parametric Study for Cost\* Optimization (VT Student Design Project)

	Preferred Concept	TS 6	TS 7	TS 8	TS 9	TS 10
Fuel Type	H2	H2	H2	H2	H2	H2
Loiter Velocity (kts)	150	200	200	200	150	175
Altitude (ft)	60000	65000	60000	65000	60000	65000
Endurance (days)	8	10	8	8	11	11
Payload (lbs)	2000	2000	3000	3000	2000	2000
TOGW (lbs)	13159	20186.21	20591.96	19206.49	14392.23	21005.86
Fuel Weight (lbs)	3878	8375.24	7677.5	6761.95	4658.48	8960.13
Aspect Ratio	40	40	40	40	40	30
Wing Span (ft)	260	260	260	260	260	260
Wing Area (square ft)	1690	1690	1690	1690	1690	2253.33
Wing Loading (psf)	7.79	11.94	12.18	11.36	8.52	9.32
Lift Coefficient (Loiter)	1.08	1.18	0.95	1.12	1.18	1.2
Loiter Power Required (hp)	115.46	245.04	226.66	236.86	129.62	279.14
Climb Power Required (hp)	314.85	550.89	538.66	527.87	347.69	597.41
Cruise Velocity (kts)	150	150	150	150	100	100
Aircraft per System	2	2	2	2	2	2
<b>Cost (millions)</b>	157.71	252.82	258.19	246.39	166.23	237.31

**\*Cost was the key Measure of Merit (MoM)**



# Example of Parametric Study for Cost\* Optimization

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*Look at the number of significant figures for some parameters, e.g., TOGW, Wing Loading. See anything wrong?*

\*Cost was the key Measure of Merit (MoM)



# Visual Display of Results

“Optimum”

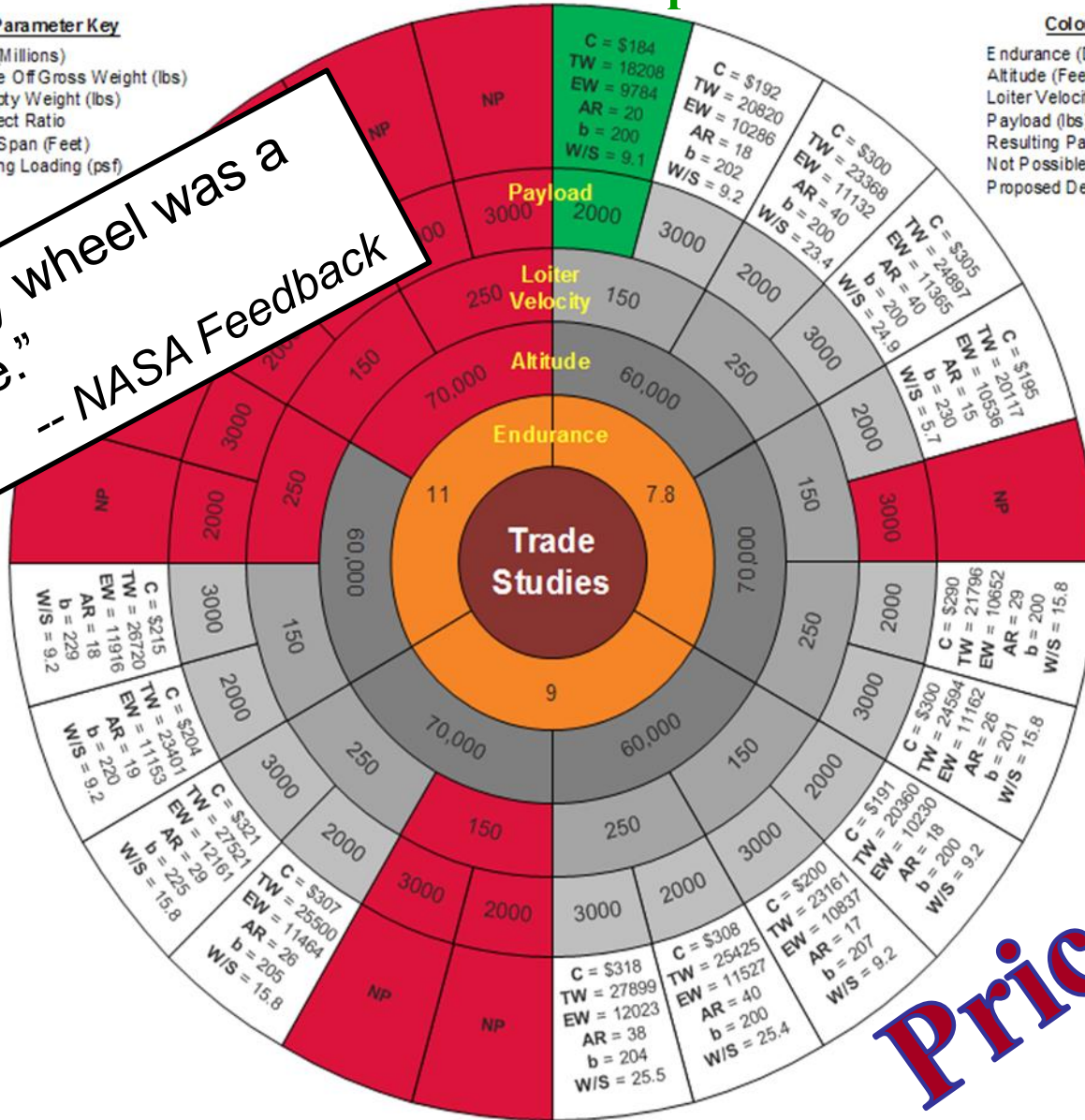
**Parameter Key**

- C - Cost (Millions)
- TW - Take Off Gross Weight (lbs)
- EW - Empty Weight (lbs)
- AR - Aspect Ratio
- b - Wing Span (Feet)
- W/S - Wing Loading (psf)

**Color Key**

- Endurance (Days) █
- Altitude (Feet) █
- Loiter Velocity (Knots) █
- Payload (lbs) █
- Resulting Parameters █
- Not Possible █
- Proposed Design █

“Trade study wheel was a great figure.”  
-- NASA Feedback



Priceless!



# Outline

## A8. Trade Studies

A8.1 General Remarks

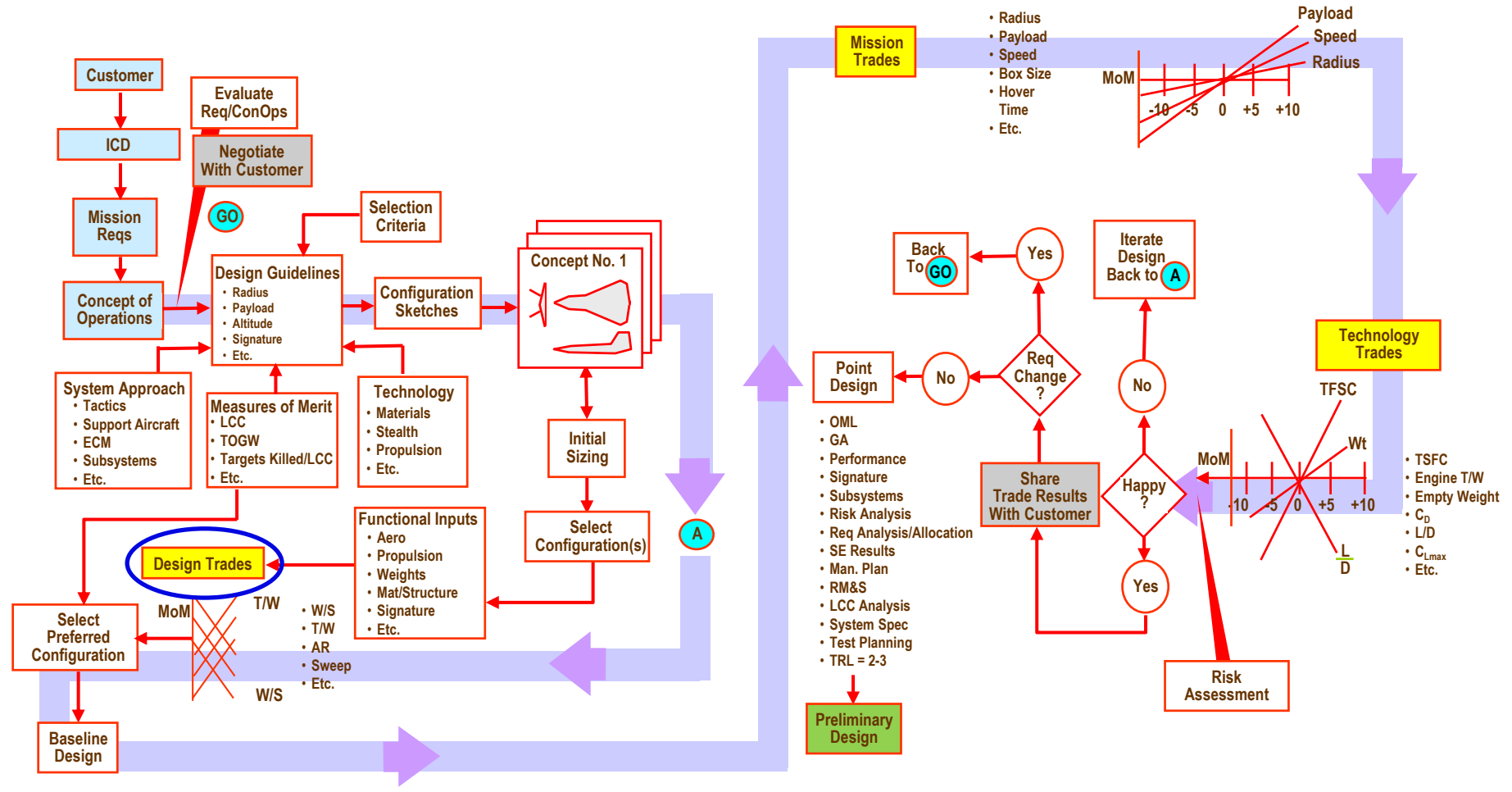
**A8.2 Design (or Configuration) Trades**

A8.3 Mission Trades

A8.4 Technology Trades

A8.5 Carpet Plot Technique

# Types of Trade Studies in Aircraft Conceptual Design



**Trade Studies help you select parameters for best design**

# Design Trades (aka Configuration Trades)

**What would be the impact on MoM if design features were changed?**

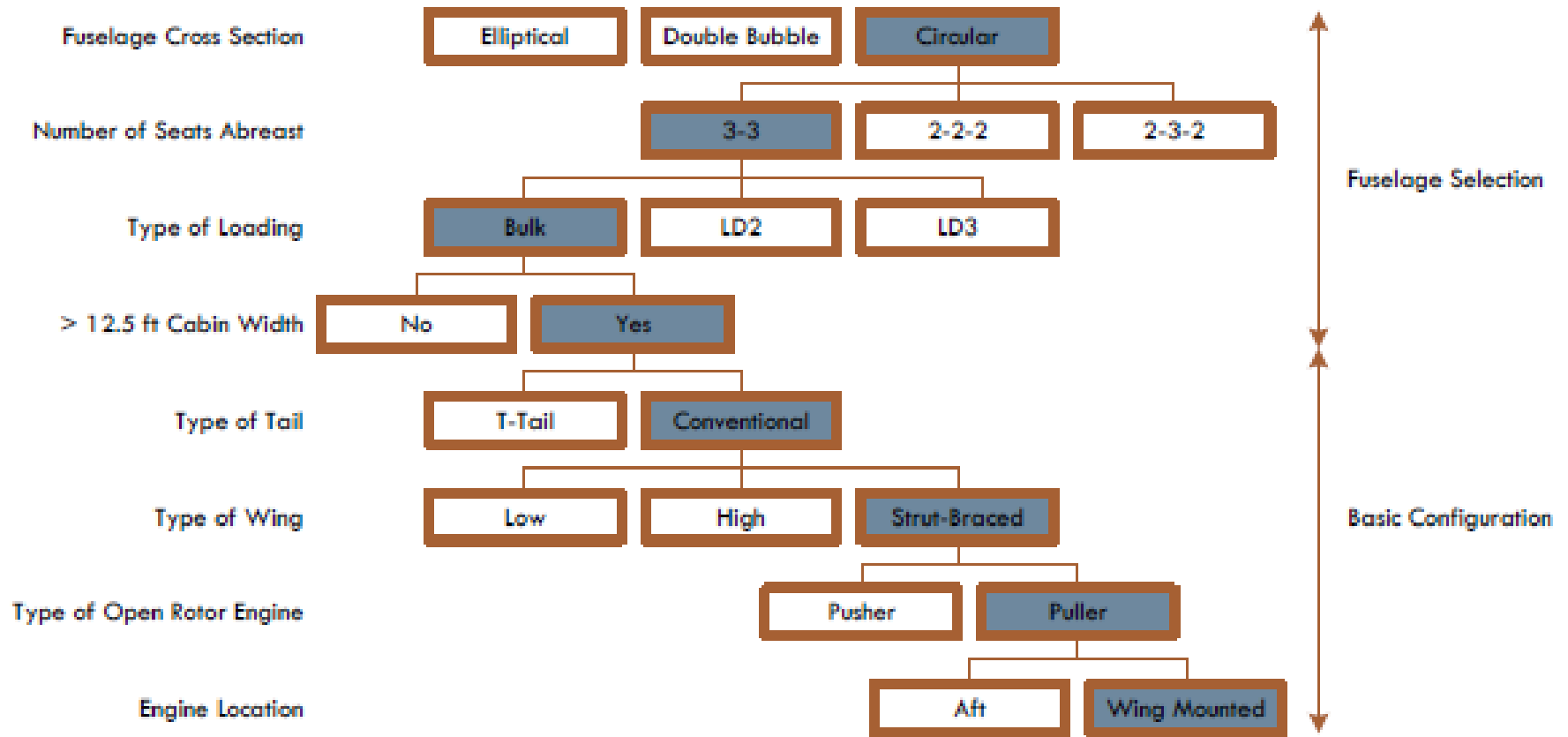
## Examples of Design Features

- Wing size (affects wing loading)
- Wing shape (sweep,  $AR$ , taper ratio, etc.)
- High-lift devices (mechanical vs. powered)
- Fuselage size and shape (fineness ratio, cross-sectional area distribution, etc.)
- Tail configuration (aft tail, canard, tailless)
- Stability level (degree of static margin)
- Engine (turboprop, turbofan, turbojet, number of engines, bypass ratio, podded or buried, etc.)
- Inlet and nozzle (location, type)
- Materials (metals or composites)
- ...

***Design Trades facilitate selection of the right combination of design features for the most efficient vehicle to meet MoMs***



# Example: Critical Design Choices for Configuration Down-selection

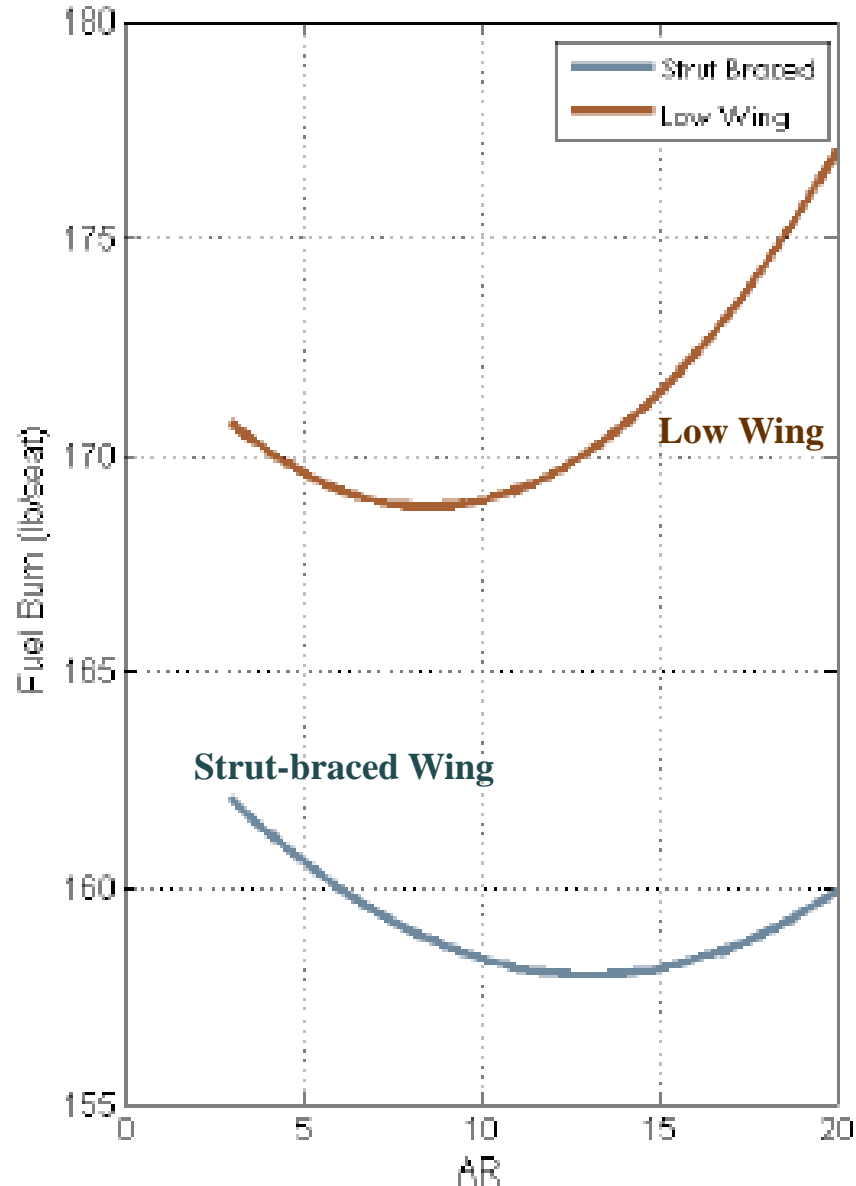


Source: 2009-10 AIAA UG Team Aircraft Design Winning Team, Cal Poly, SLO

# Example: Best $AR$ for Fuel Efficiency

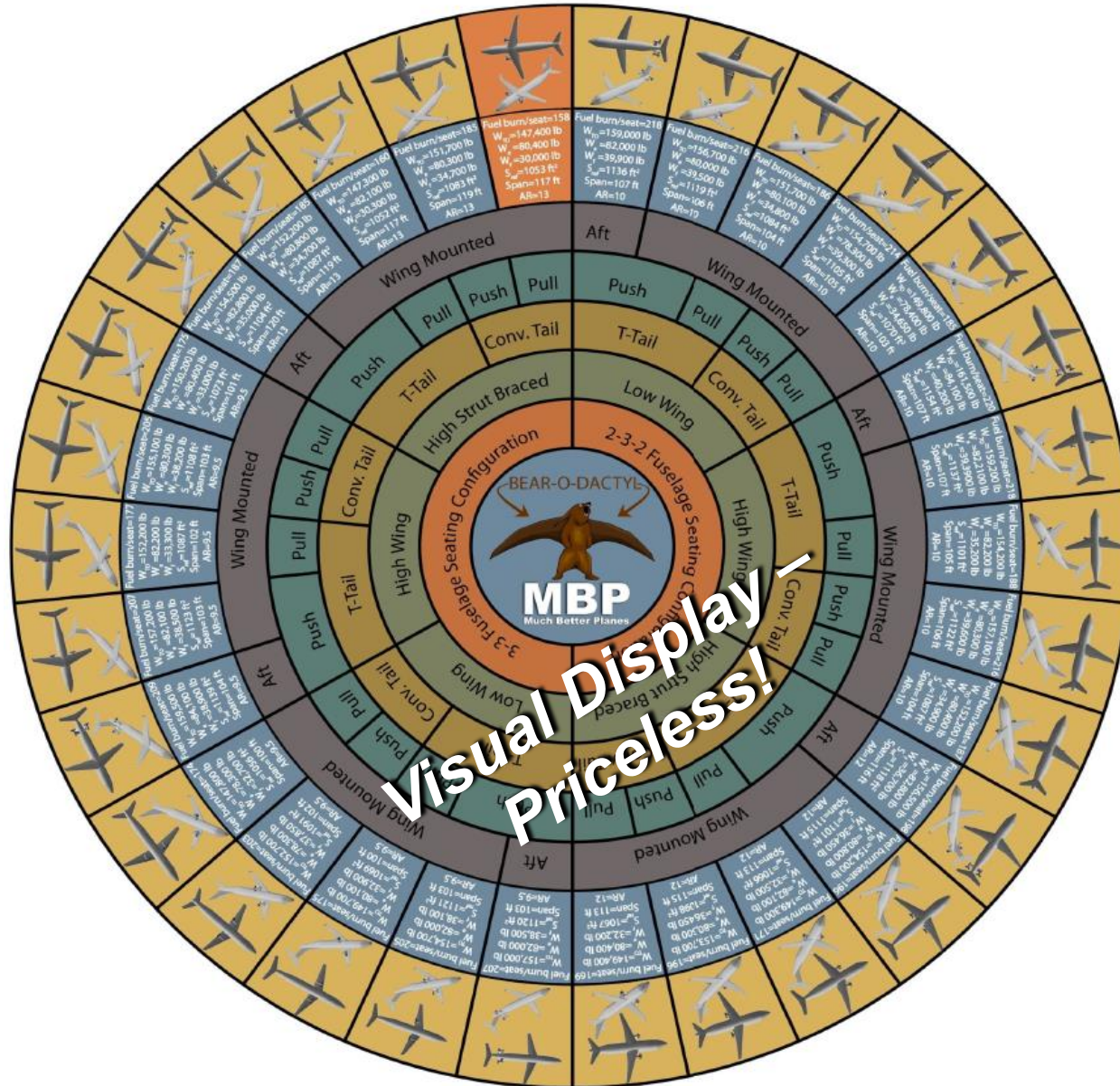
## Design Objective

***Minimize Fuel  
 Burn for a  
 Passenger  
 Transport  
 Aircraft***



Source: 2009-10 AIAA UG Team Aircraft Design Winning Team, Cal Poly, SLO

# Example of Configuration Trade Study



Source: 2009-10 AIAA UG Team Aircraft Design  
Winning Team, Cal Poly, SLO



# Outline

## A8. Trade Studies

A8.1 General Remarks

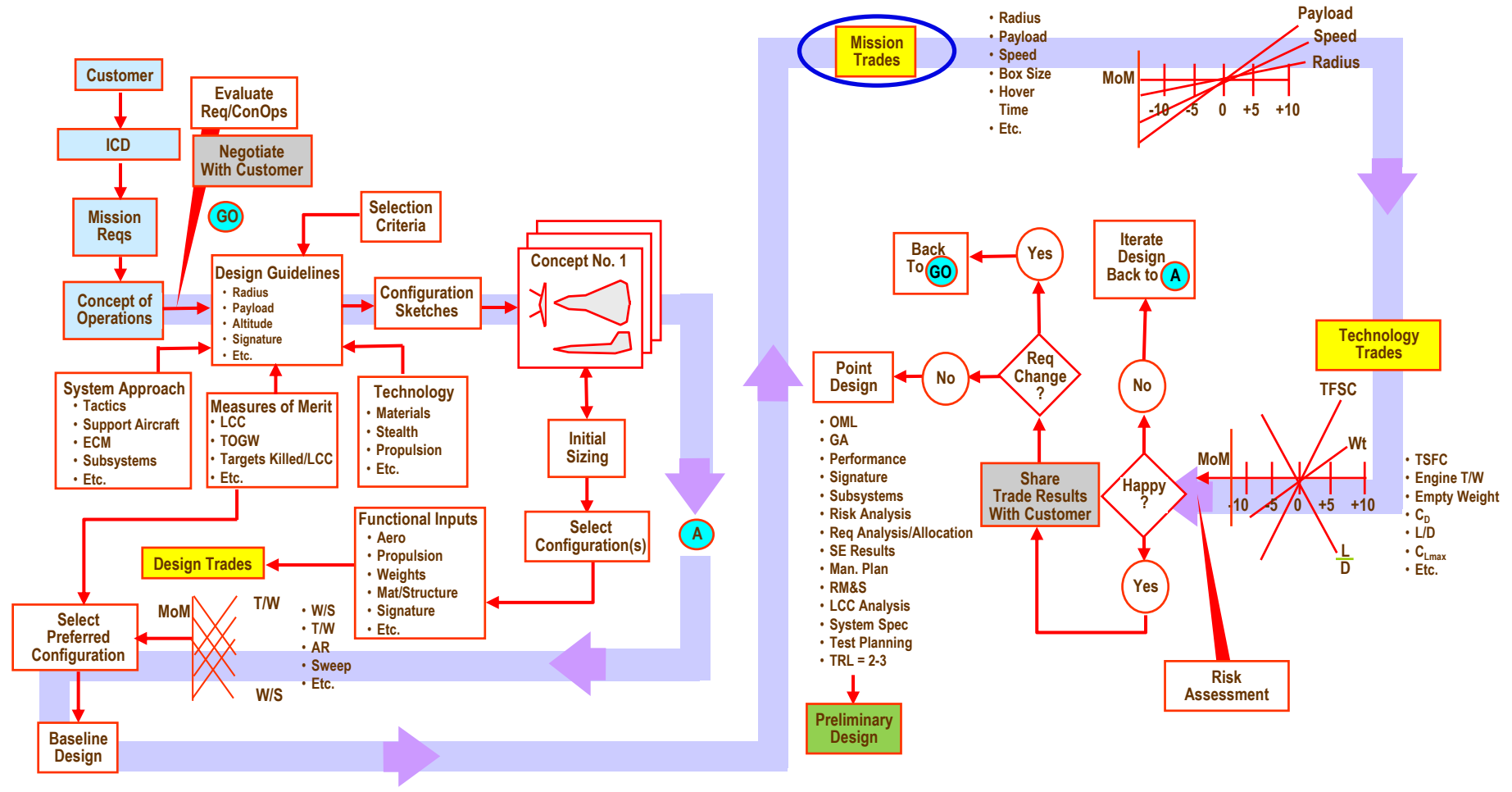
A8.2 Design (or Configuration) Trades

**A8.3 Mission Trades**

A8.4 Technology Trades

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# Types of Trade Studies in Aircraft Conceptual Design



**Trade Studies help you select parameters for best design**

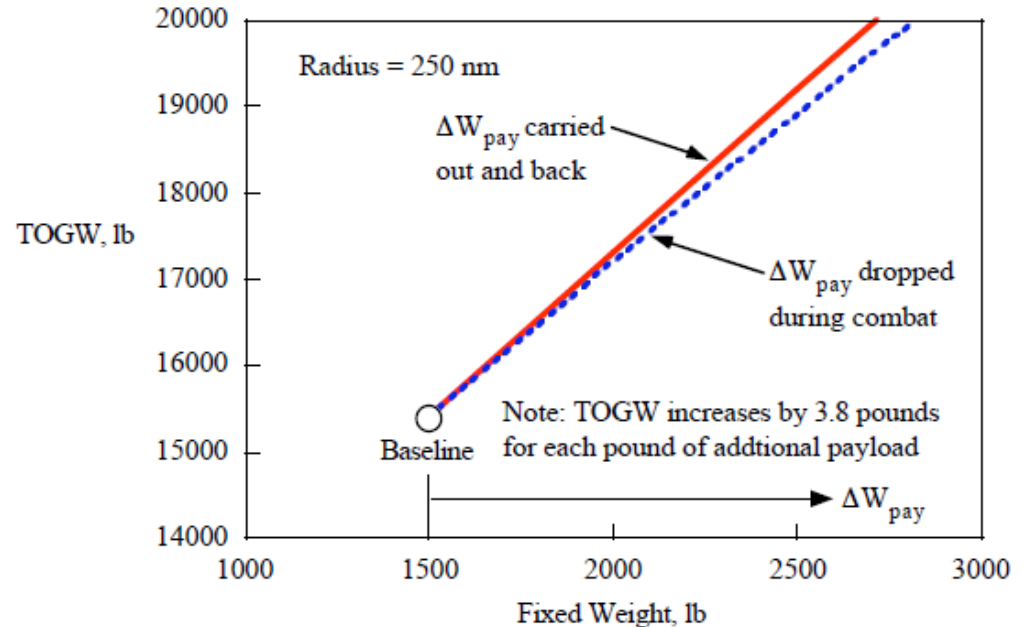
# Mission Trades

**What would be the impact on TOGW if we changed Payload ( $\pm 25\%$ ), Range ( $\pm 25\%$ ), Endurance ( $\pm 25\%$ ), etc.?**

- Trade Study of TOGW for varying fixed weight gives weight sensitivity ratio,  $\Delta W_{TO} / \Delta W_{payload}$ , of 3.8!
- It is also called **aircraft growth factor**.
  - Typically, larger the payload fraction, larger the growth factor.

Example:

$W_{TO}$  Variation with Payload for Fixed Radius

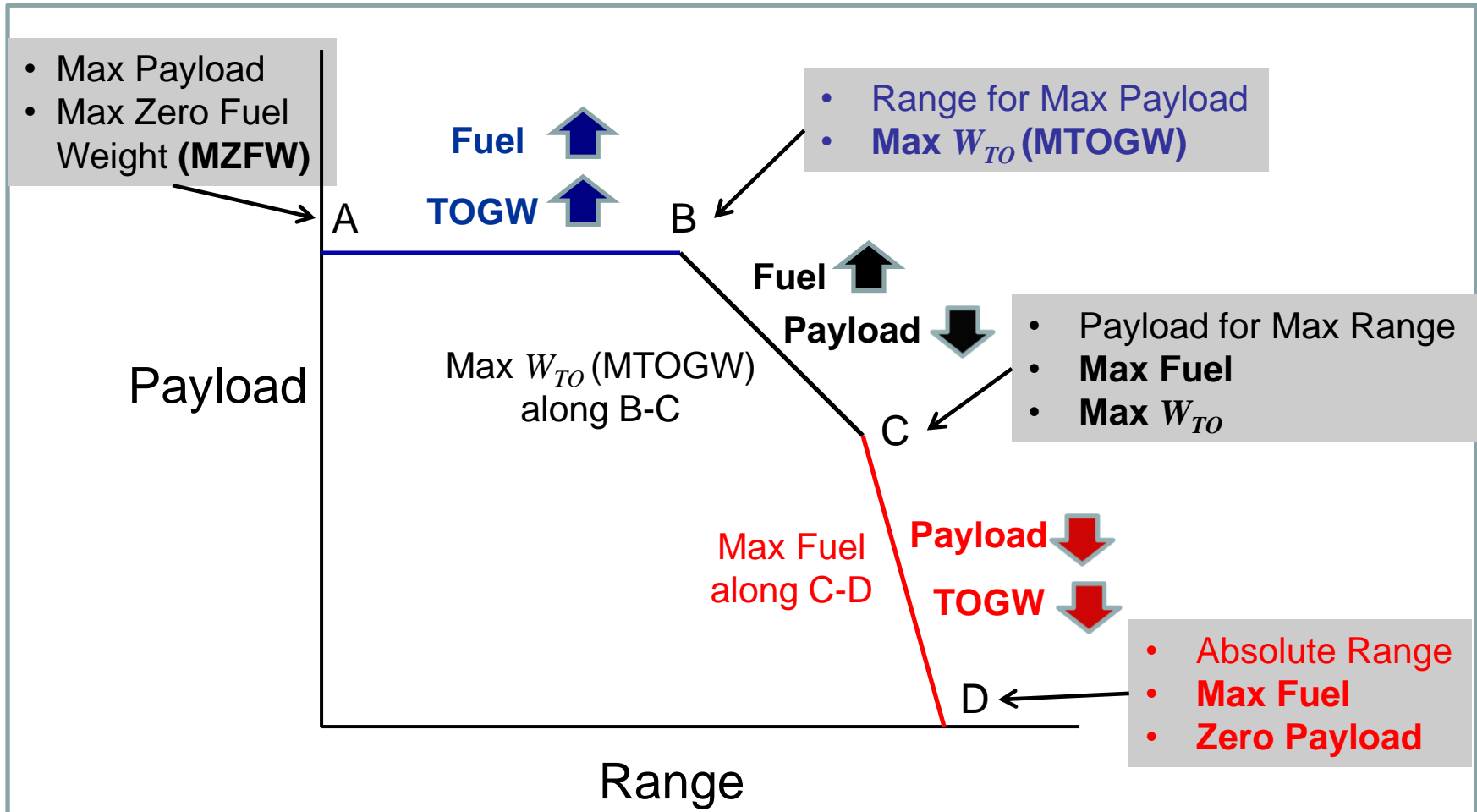


Source: Fig. 5.6, Ref. AVD 1 (Nicolai and Carichner)

- Use Mission Trade results to *identify requirements* that might be dominant design drivers—the ones to which TOGW is most sensitive.

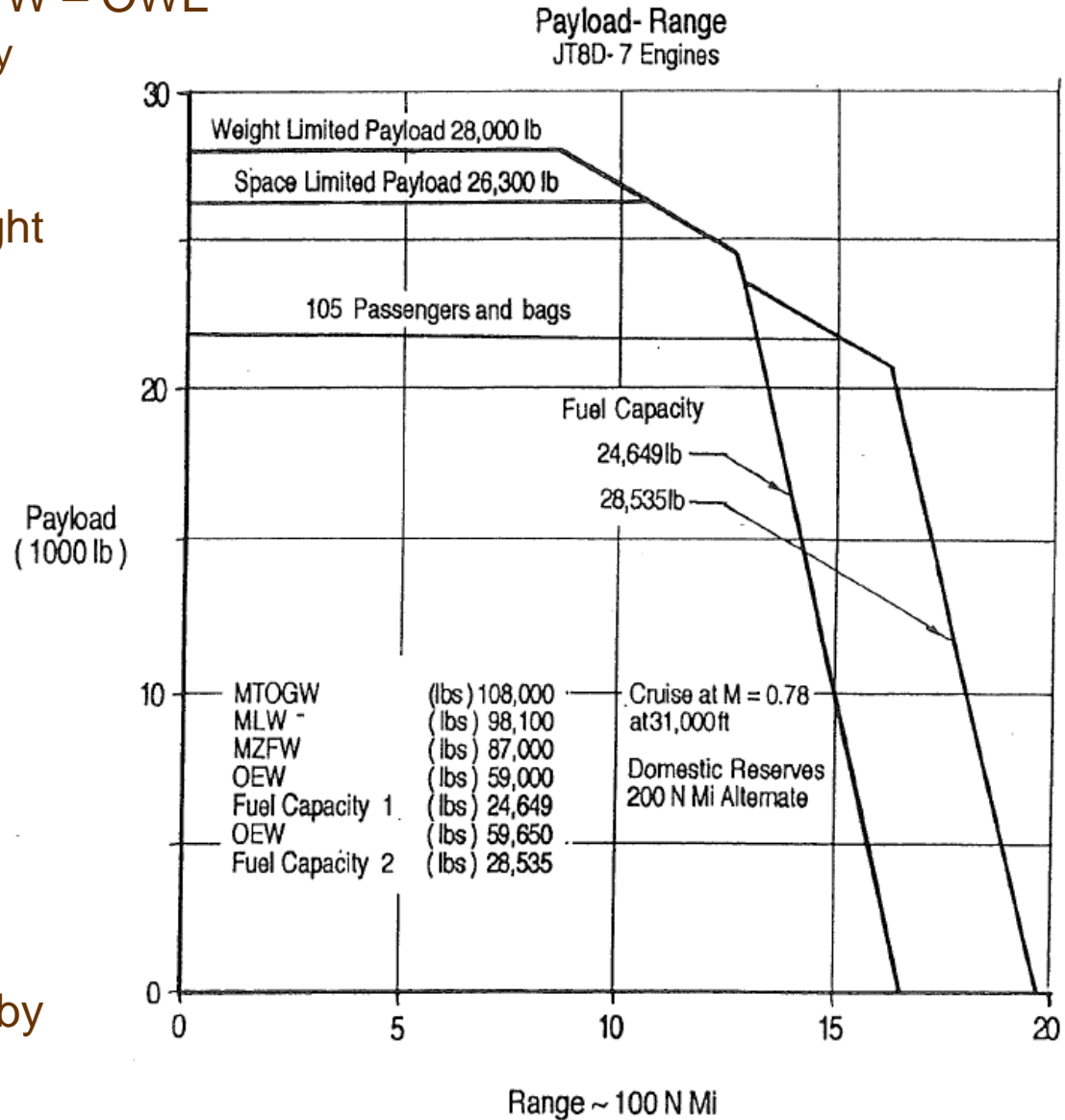
# Payload-Range Trade

- Conducted for aircraft with range or payload as key drivers
- Payload-Range plots that are useful for interactions with customers; may be helpful in “refining” requirements



# A Typical Payload-Range Curve

- Weight Limited Payload = MZFW – OWE
  - Space-limited payload is usually
  - slightly lower
- MZFW = MTOGW – Fuel Weight
- $OWE = W_{empty} + W_{nonexpendables}$ 
  - 2<sup>nd</sup> term covers Operational Items such as crew
  - No payload or cargo or fuel
- MTOGW sets the range based on (passengers + bags) payload
- Greater range for the same amount of (passenger + bags) payload can be achieved only by increasing fuel capacity



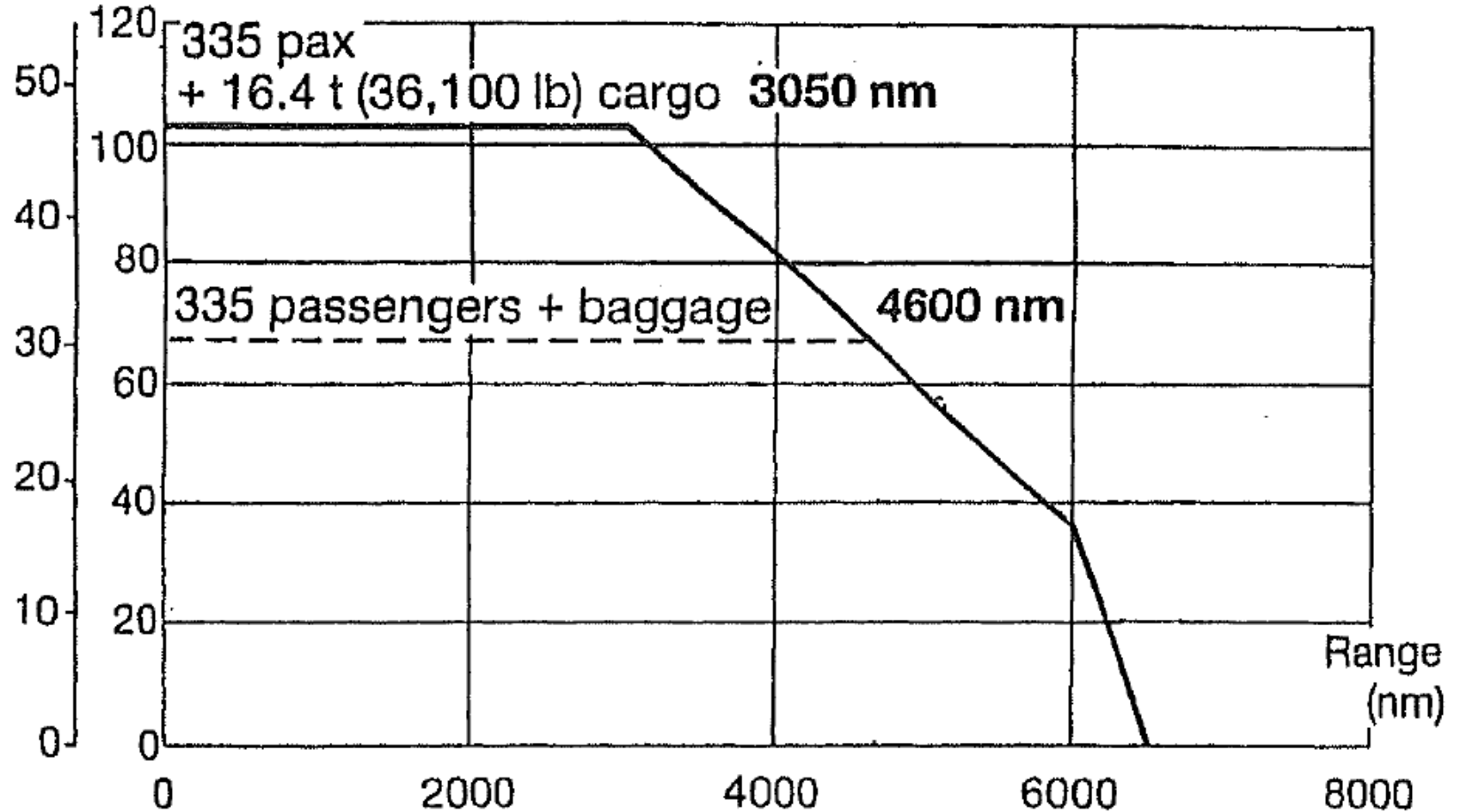


# A330-300 Payload-Range Capability

**GE CF6-80E1A1**

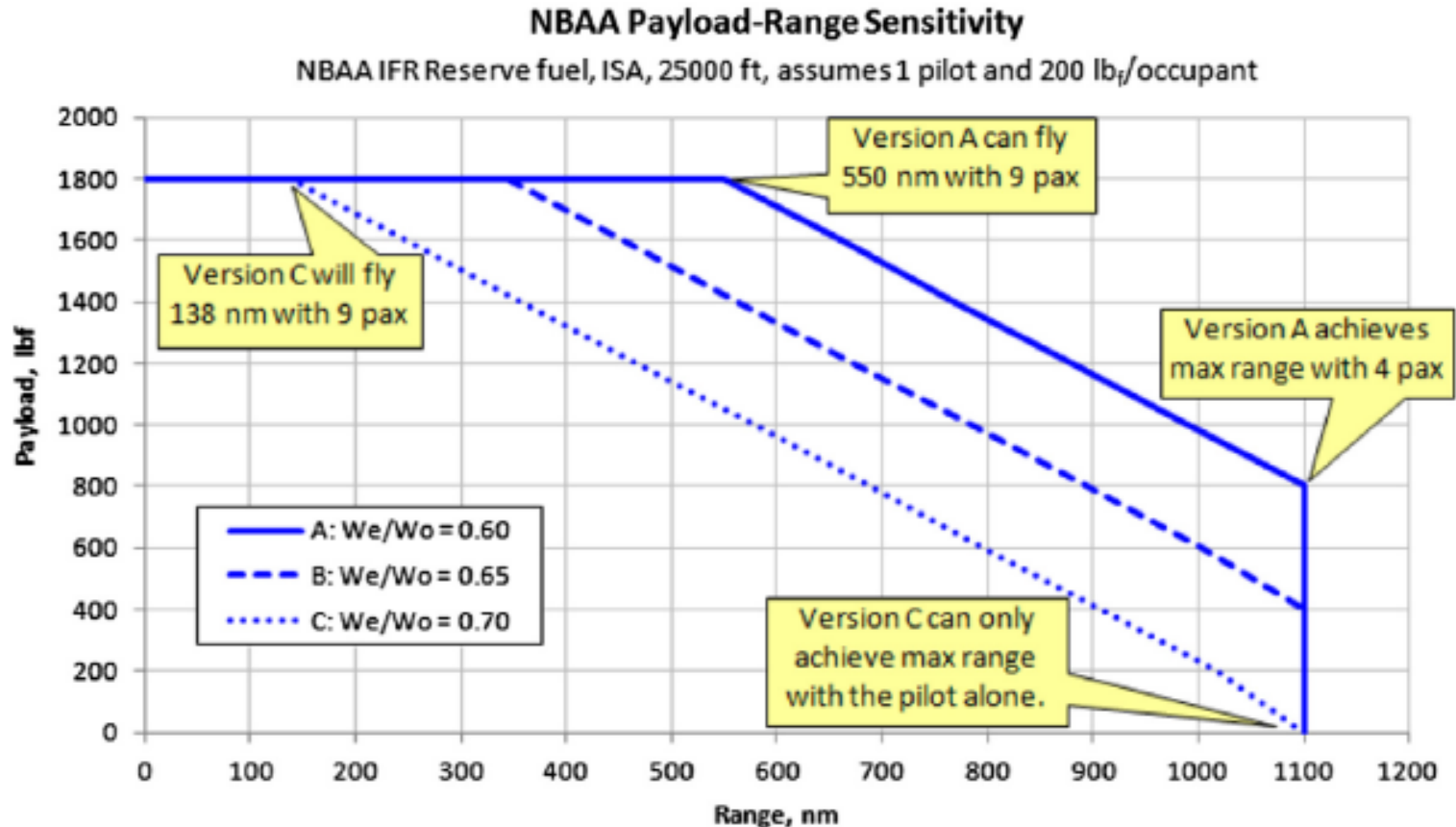
Typical international reserves  
 200 nm alternate  
 Typical Airline OWE

Payload  
 (tonnes) (1000 lb)



# Payload-Range Parametric Study

- Nine-passengers, each 200 lb<sub>f</sub>
- Maximum TOGW of 7,500 lb<sub>f</sub> & max fuel weight of 2,000 lb<sub>f</sub>



***Empty Weight would be a dominant design driver!***



# Outline

## A8. Trade Studies

A8.1 General Remarks

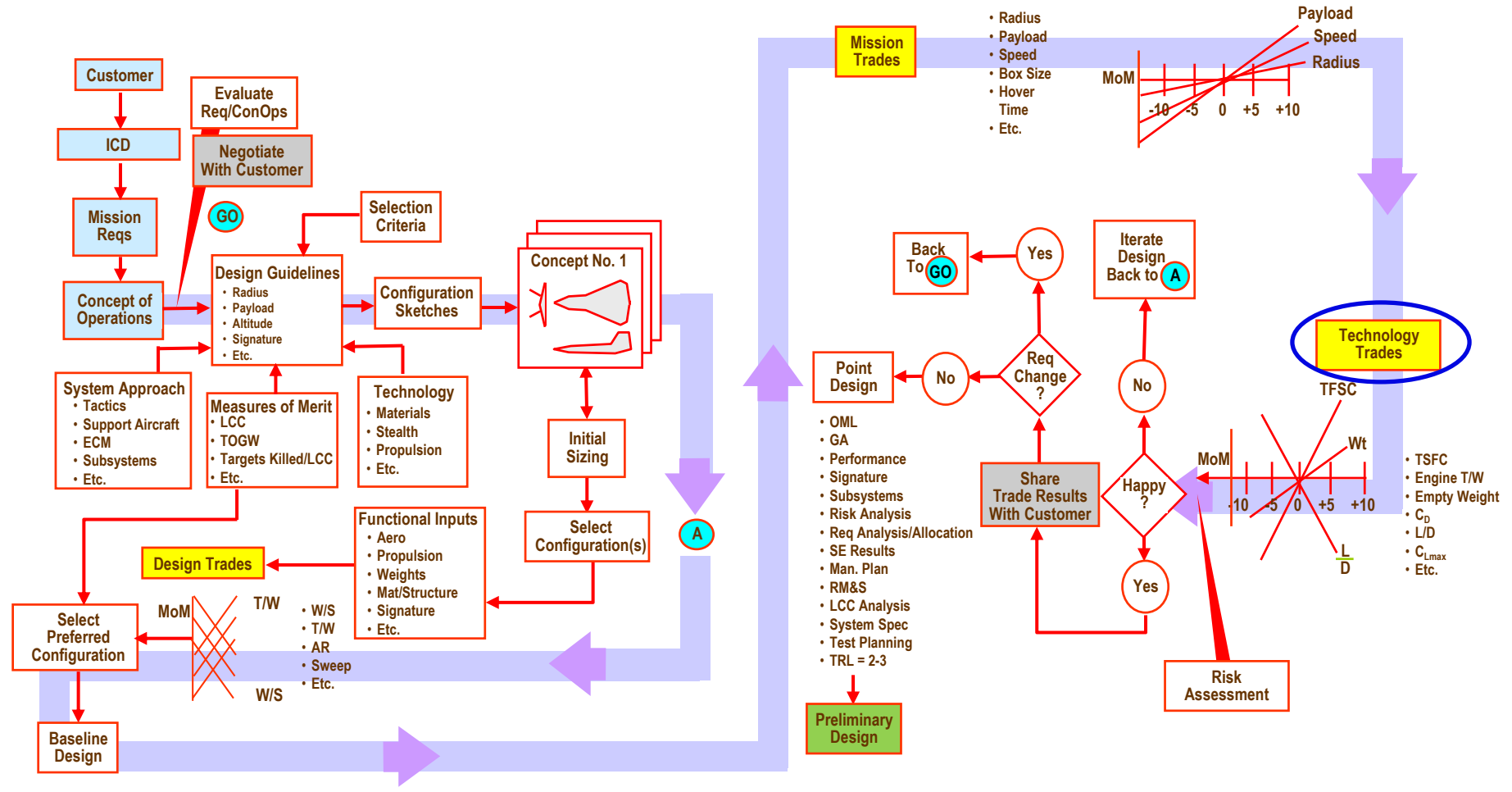
A8.2 Design (or Configuration) Trades

A8.3 Mission Trades

**A8.4 Technology Trades**

A8.5 Carpet Plot Technique

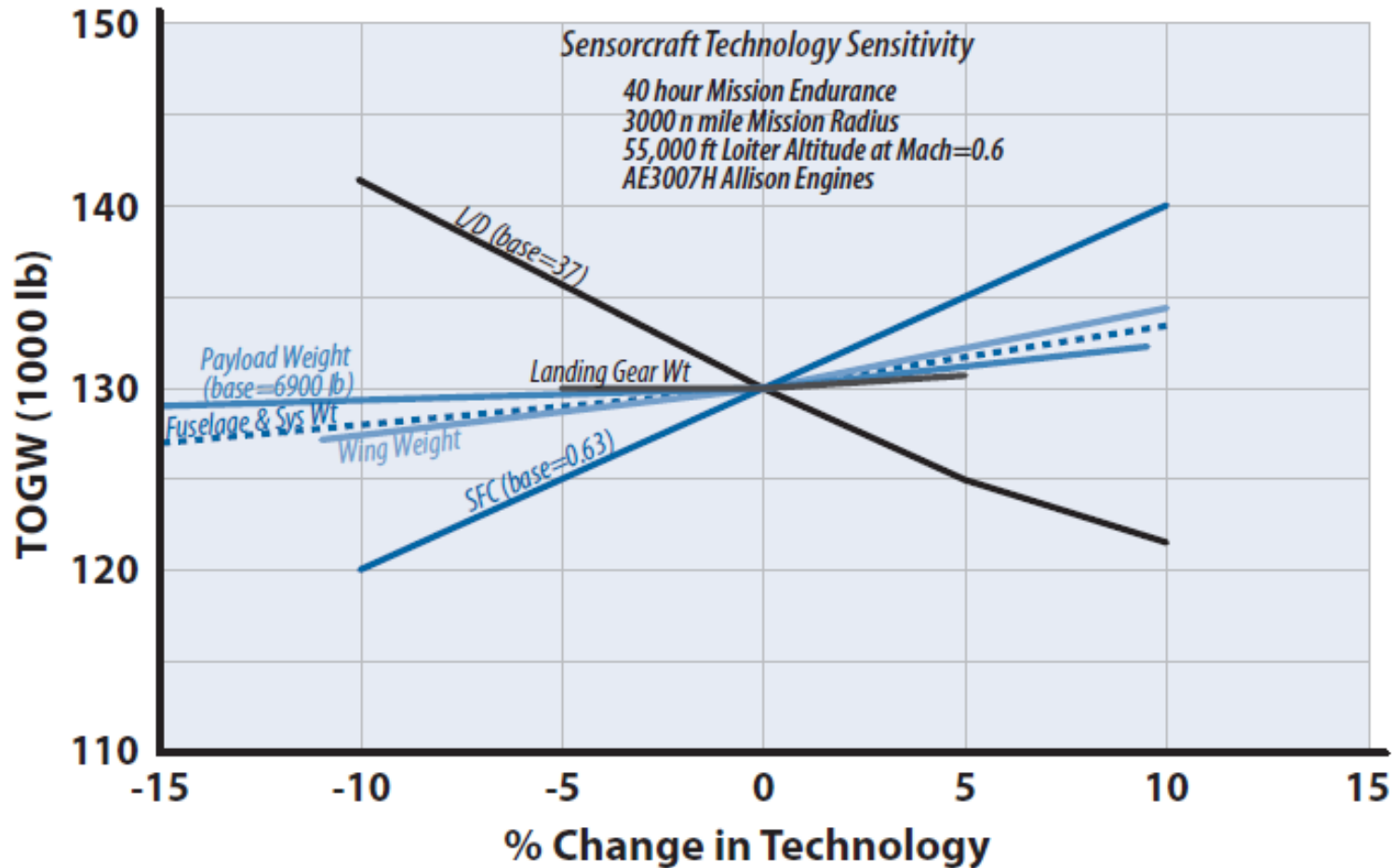
# Types of Trade Studies in Aircraft Conceptual Design



**Trade Studies help you select parameters for best design**

# Technology Trades

***What would be the impact on TOGW (or some other MoM) if we could change L/D ( $\pm 10\%$ ), sfc ( $\pm 10\%$ ), Wing Weight ( $\pm 10\%$ ), etc., etc.?***

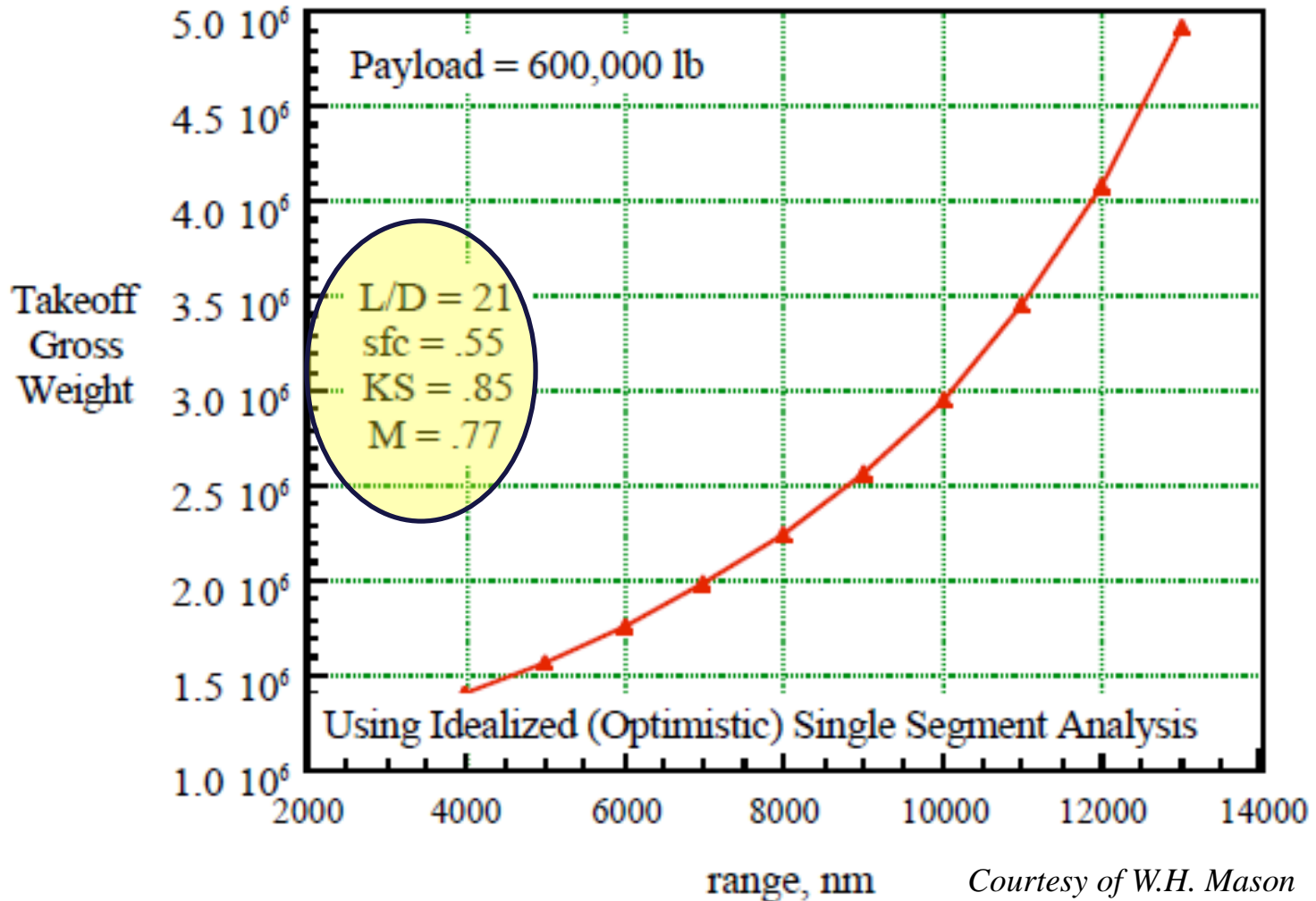


Source: Fig. 25.7, Ref. AVD 1 (Nicolai and Carichner)

# Benefits of Technology Trades

- **Technology Trades provide a basis for Risk Analysis**
  - Consequence (or impact) of technology failing to perform
  - Probability of technology failing to perform
- **Results useful for Technology Investment Planning**
  - Payoffs of accelerated technology maturation

# $W_{TO}$ Variation with Range for Fixed Payload



**For a *specified technology level*, “exponential” growth in TOGW could limit maximum Range**



# Outline

## A8. Trade Studies

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**A8.5 Carpet Plot Technique**



# To facilitate learning about parametric studies for multiple independent variables...

## ...we will talk about Carpet Plots

- “The graphed values of a function of more than one variable, read from an ordinate at points located by the intersection of curves of constant values of each of the variables.” –Collins Dictionary
- A powerful techniques widely used to depict the response of a system of two or more independent variables and one or more dependent variables

### Consider an example with three parameters (*start small!*)

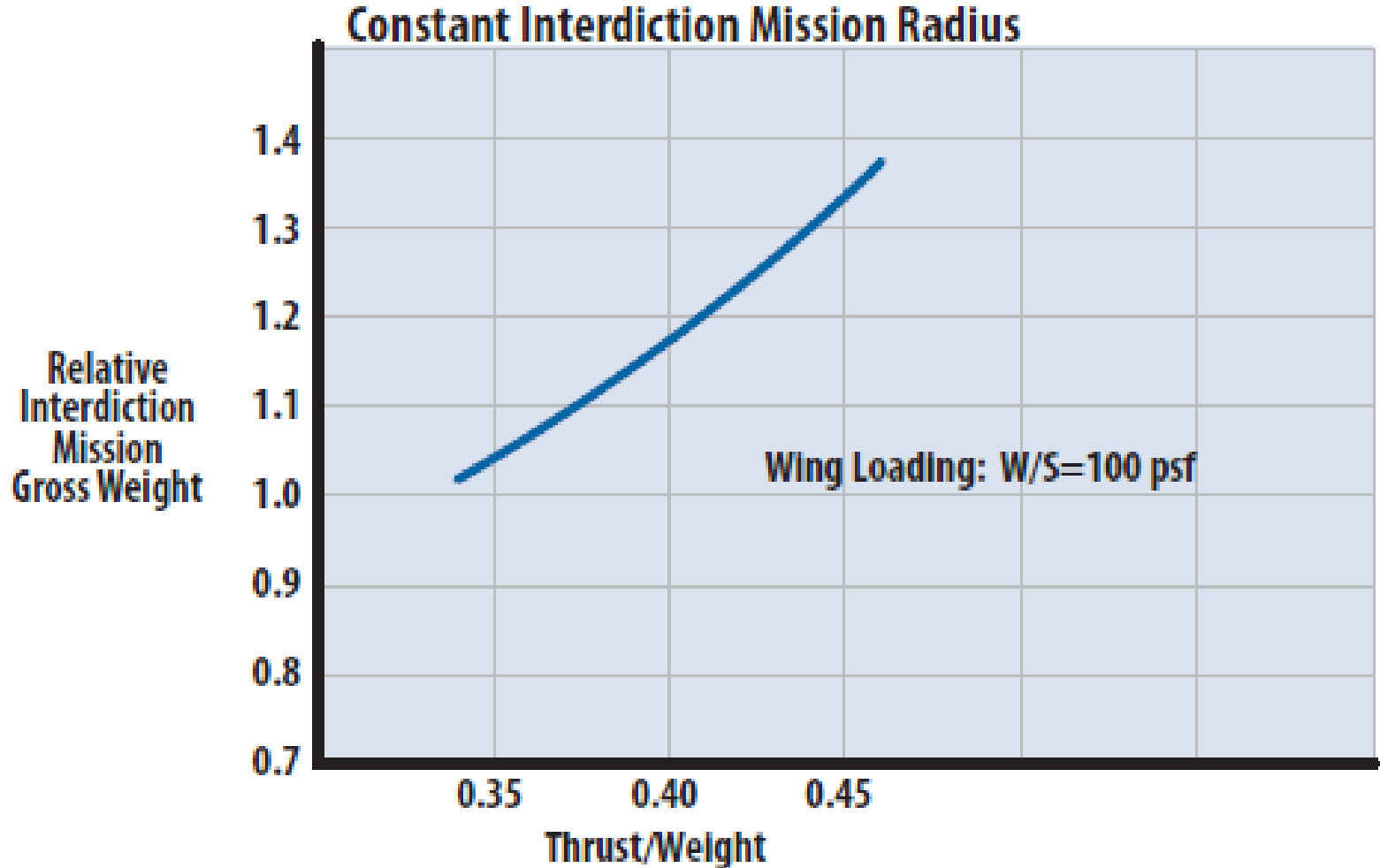
- Take-off Gross Weight,  $W_{TO}$  (*Dependent Variable*)
- Wing Loading,  $W/S$  (*Independent Variable*)
- Thrust Loading,  $T/W$  (*Independent Variable*)

### Questions to answer for this example

1. How does  $W_{TO}$  change with different combinations of  $W/S$  and  $T/W$ ?
2. What combination best meets customer needs?

# Carpet Plots: Step A (Starting Point)

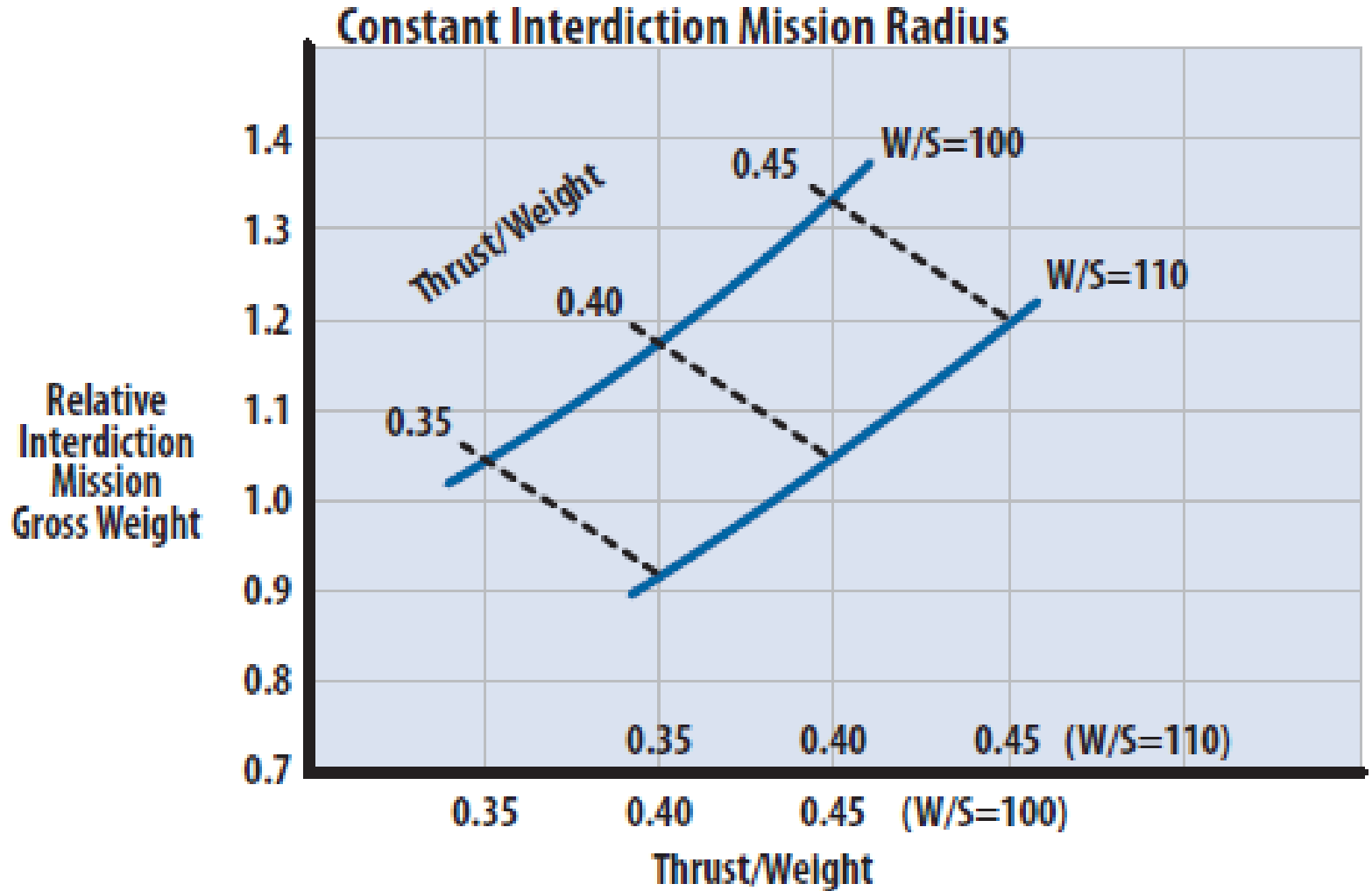
## Step A. Basic Two-variable Plot



Make Individual Plots for Several Wing-loading Values

# Carpet Plots: Step B

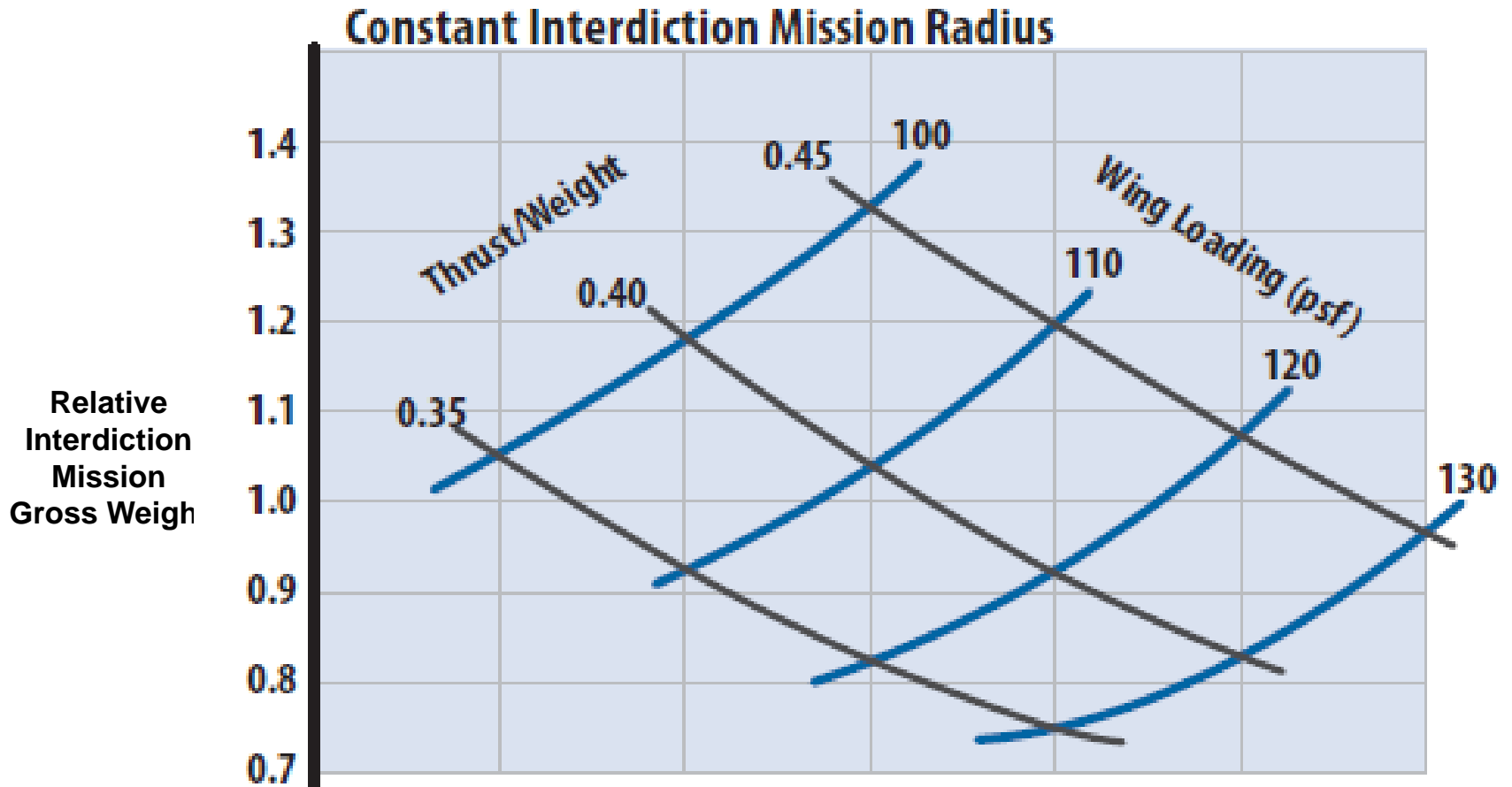
Step B. Three variables with abscissa scale shift



Source: Figure 25.3, Ref. AVD 1 (Nicolai and Carichner)

# Carpet Plots: Step C

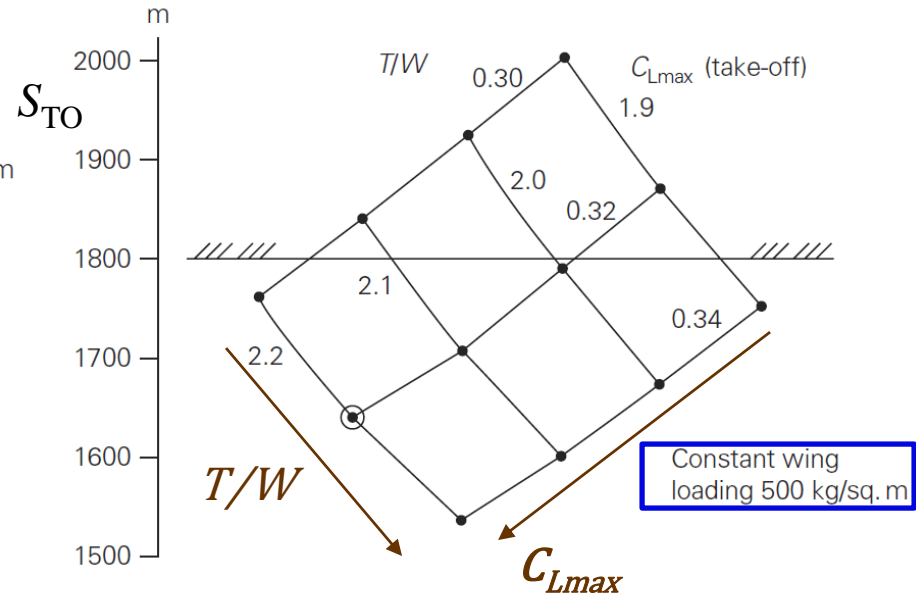
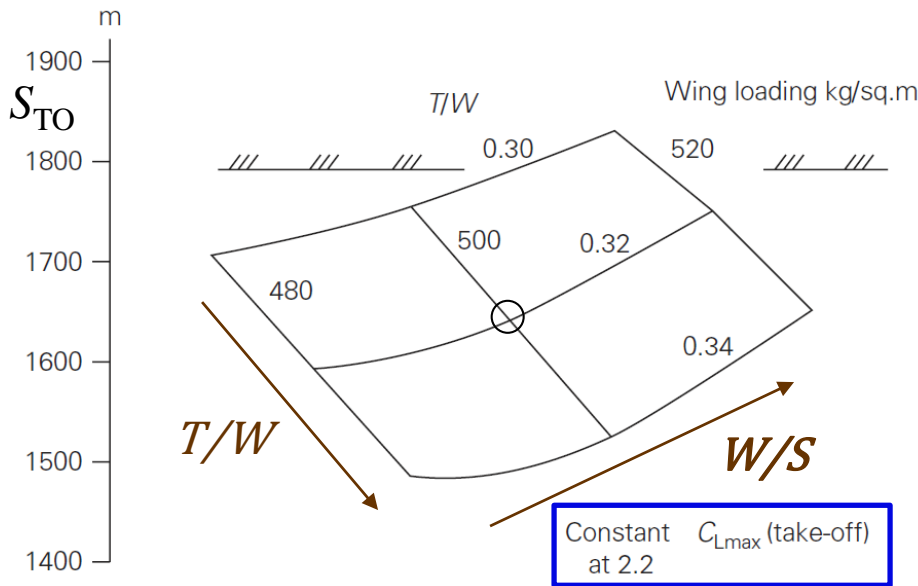
## Step C. Completed Carpet Plot



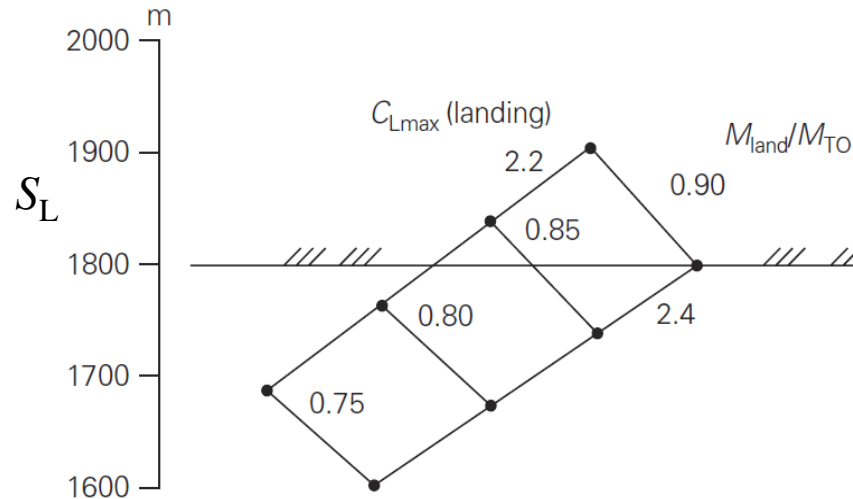
Note: *abscissa scale deleted*

# Trade Studies Example

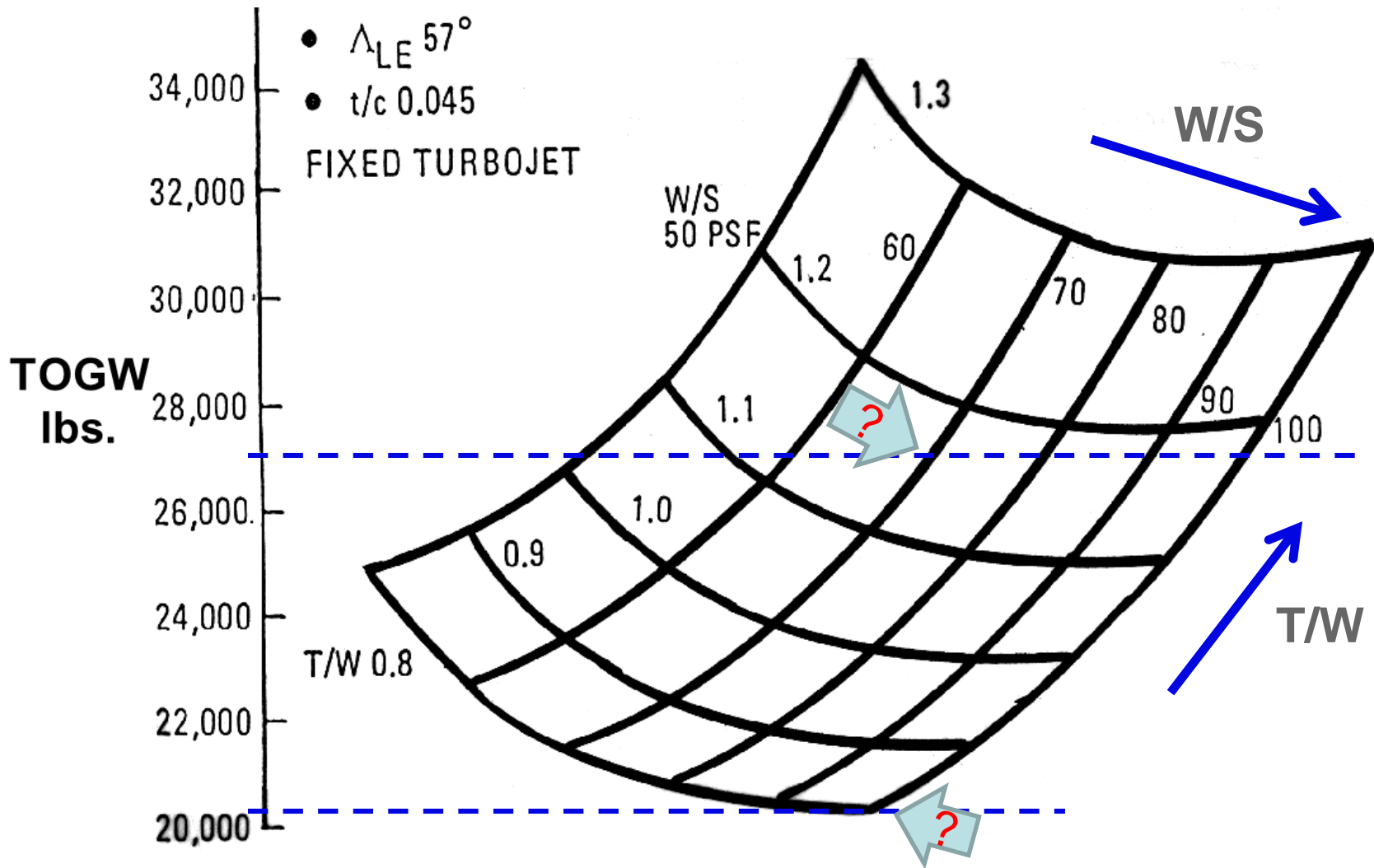
## • Take-off Parameters



## • Landing Parameters



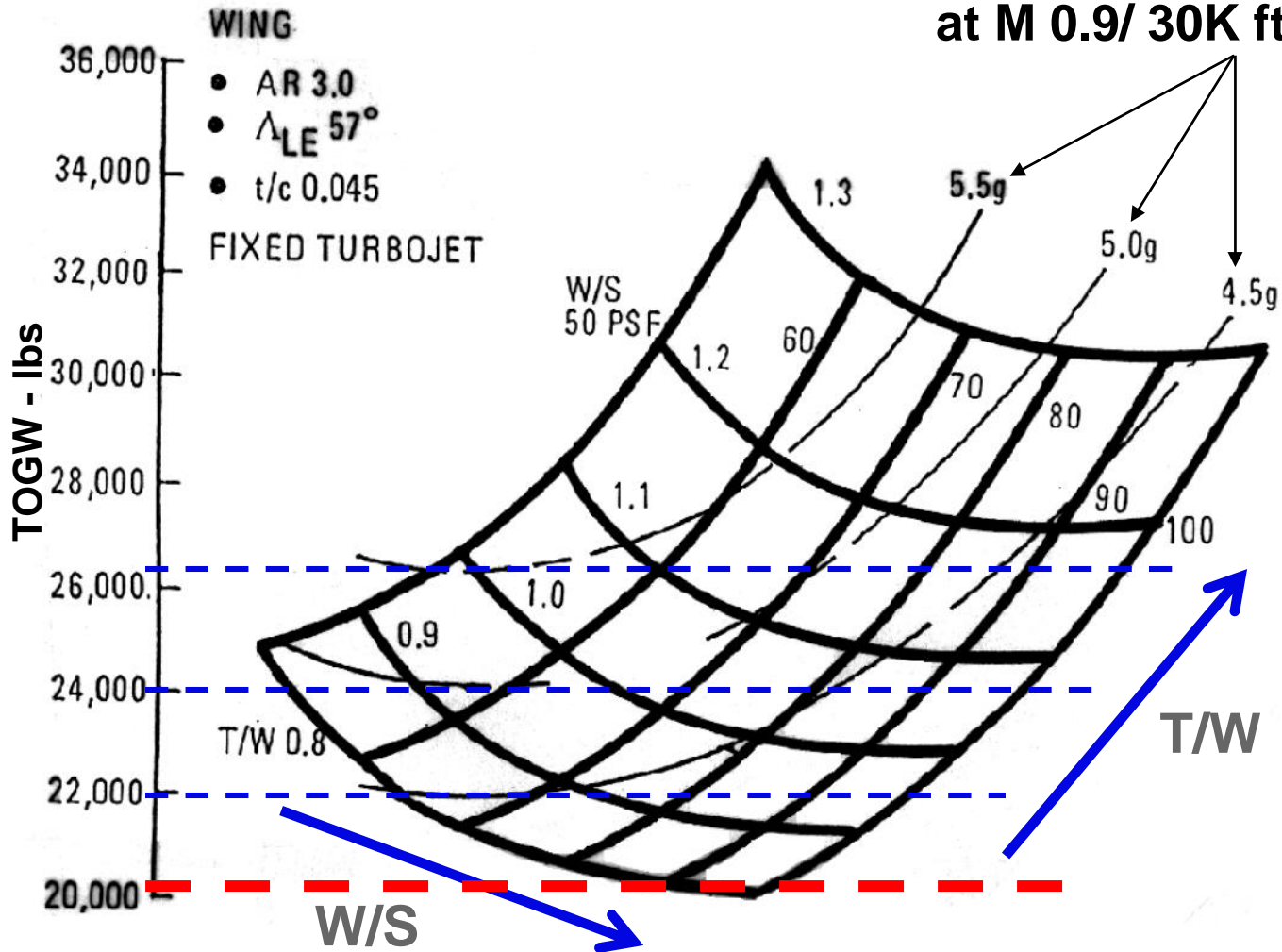
# Value of Carpet Plots: A Supersonic Fighter Example



What is the “best” combination to meet ALL requirements?

# Using a Carpet Plot: A Supersonic Fighter Example

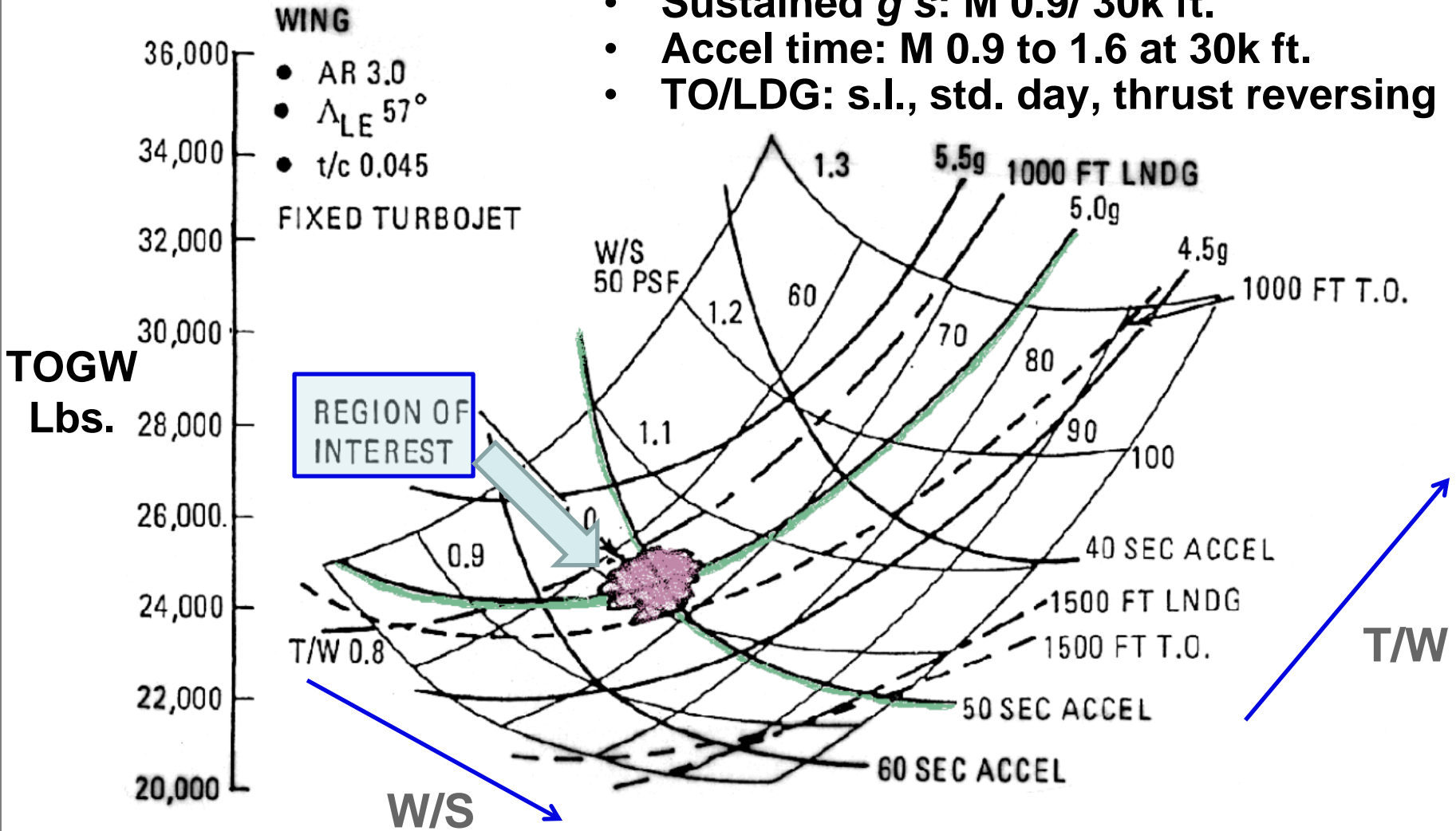
Add constraints for g's at M 0.9/ 30K ft. altitude



# Using a Carpet Plot: A Supersonic Fighter Example

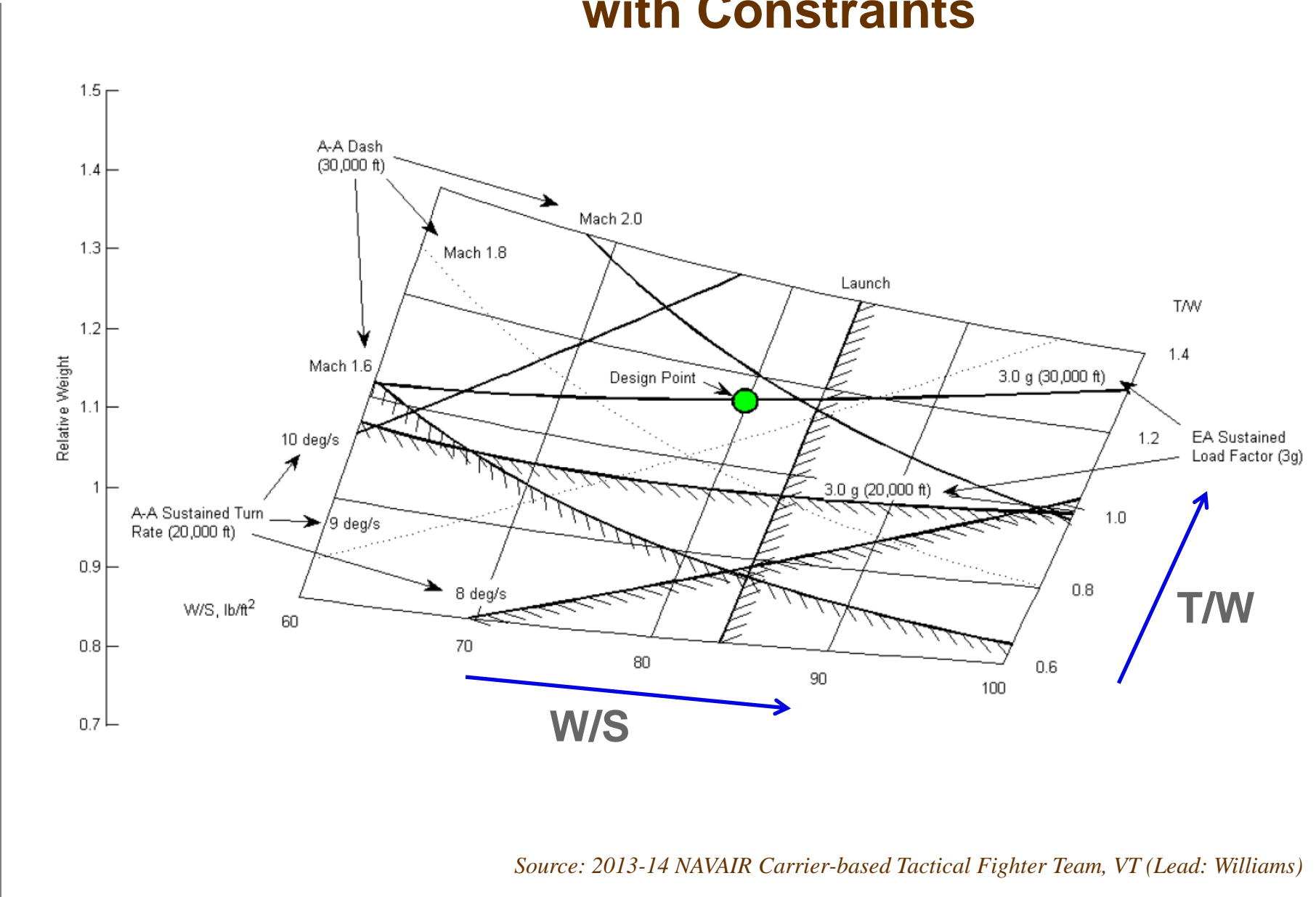
## More Constraints

- Sustained g's: M 0.9/ 30k ft.
- Accel time: M 0.9 to 1.6 at 30k ft.
- TO/LDG: s.l., std. day, thrust reversing





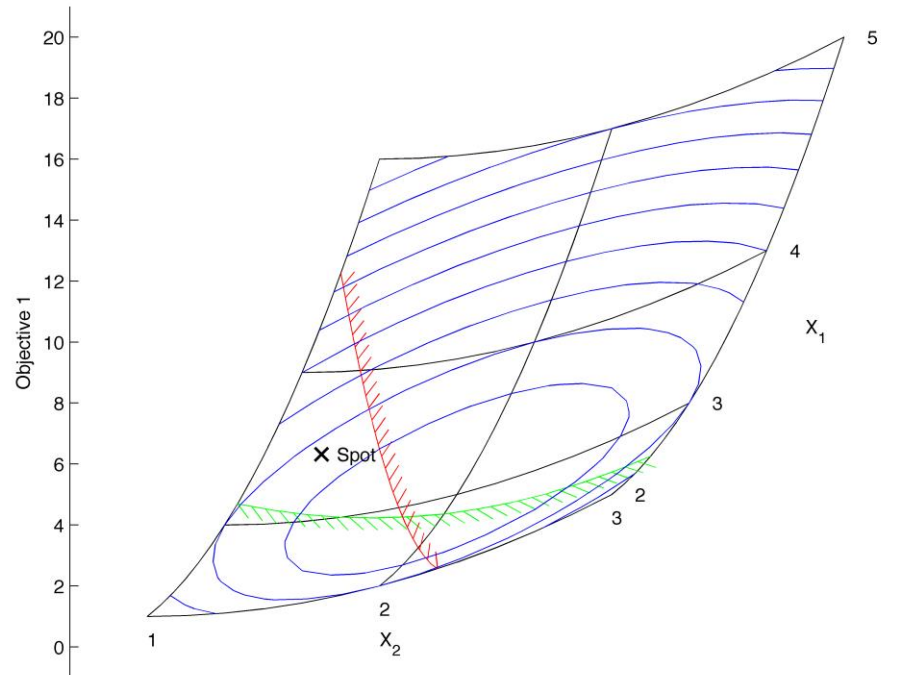
# F/A-36 Carpet Plot with Constraints



Source: 2013-14 NAVAIR Carrier-based Tactical Fighter Team, VT (Lead: Williams)

# Suggested Software for Carpet Plots

1. **Carpet Plot Toolkit, Version 1.0**, by Rob McDonald, in  MathWorks®  
<https://www.mathworks.com/matlabcentral/fileexchange/40831-carpet-plot-toolkit>



2. **Generation of Carpet Plots**, Sydney Powers

[http://www.dept.aoe.vt.edu/~mason/Mason\\_f/SD1CarpetsbySAP.pdf](http://www.dept.aoe.vt.edu/~mason/Mason_f/SD1CarpetsbySAP.pdf)

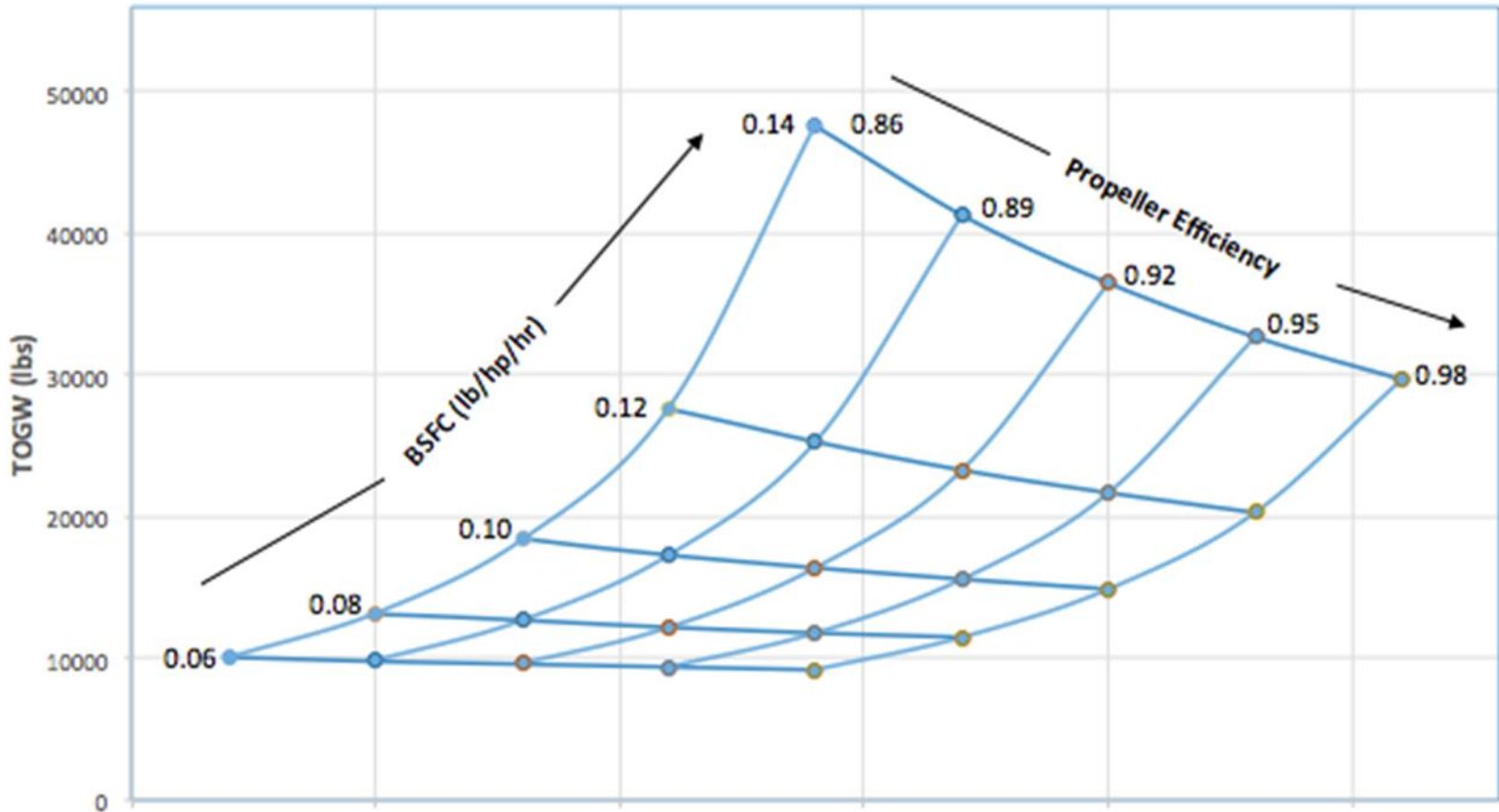
## Note:

**Carpet Plot is a general technique, not limited to just determining the best combination of  $W/S$  and  $T/W$  for minimum  $W_{TO}$  (takeoff gross weight).**

# A Three-parameter Carpet Plot

**Effect of BSFC and Propeller Efficiency on TOGW**  
**Notice different parameters (not W/S and T/W)**

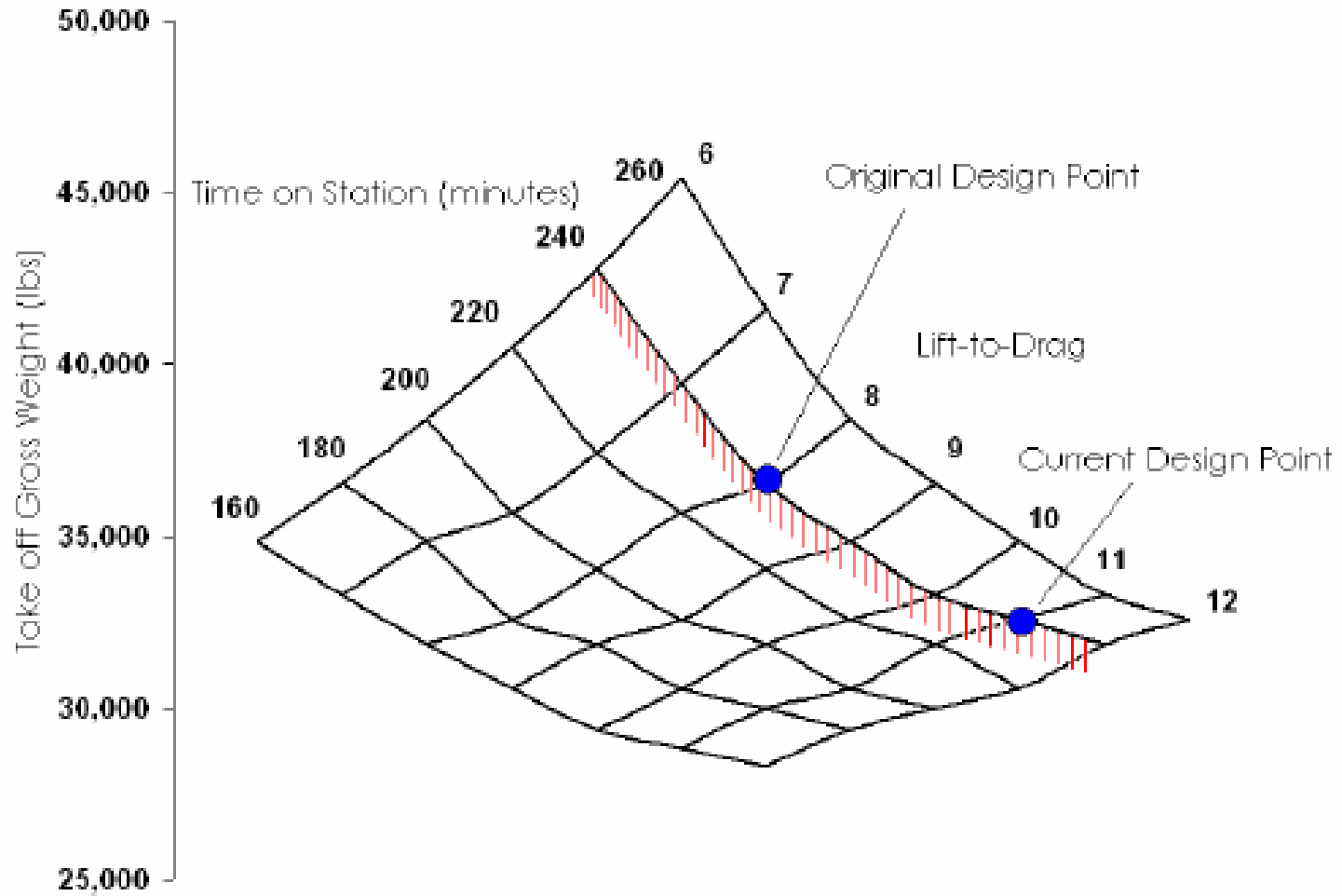
## HALE UAS Example



**Higher Sensitivity of TOGW to BSFC than Propeller Efficiency**

# A Three-parameter Carpet Plot

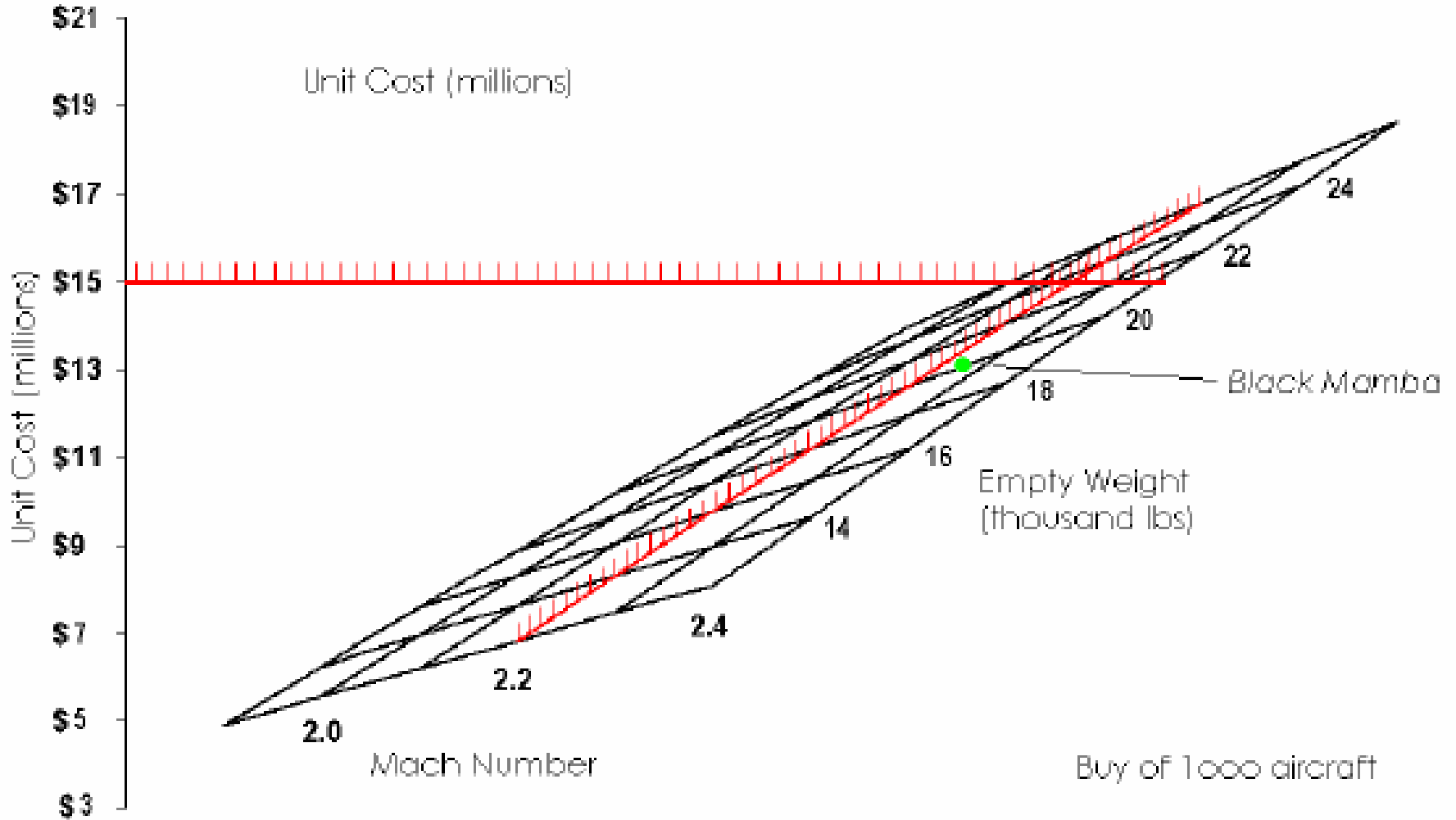
## Effect of L/D on TOGW



Source: 2005-06 AIAA Team Design, The Black Mamba, Cal Poly, SLO

# Three-parameter Carpet Plot

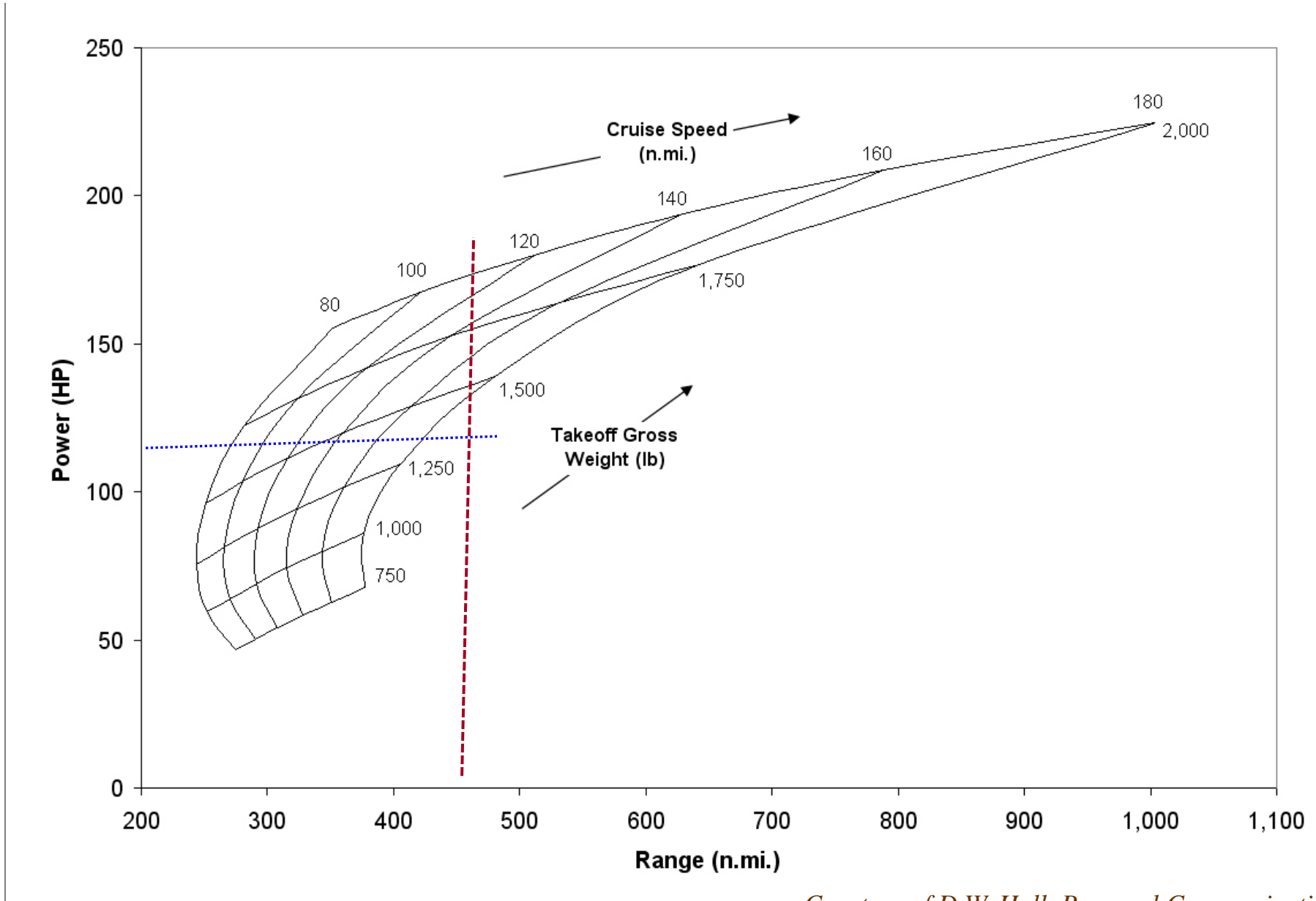
## Effect of Empty Weight and Mach Number on Cost



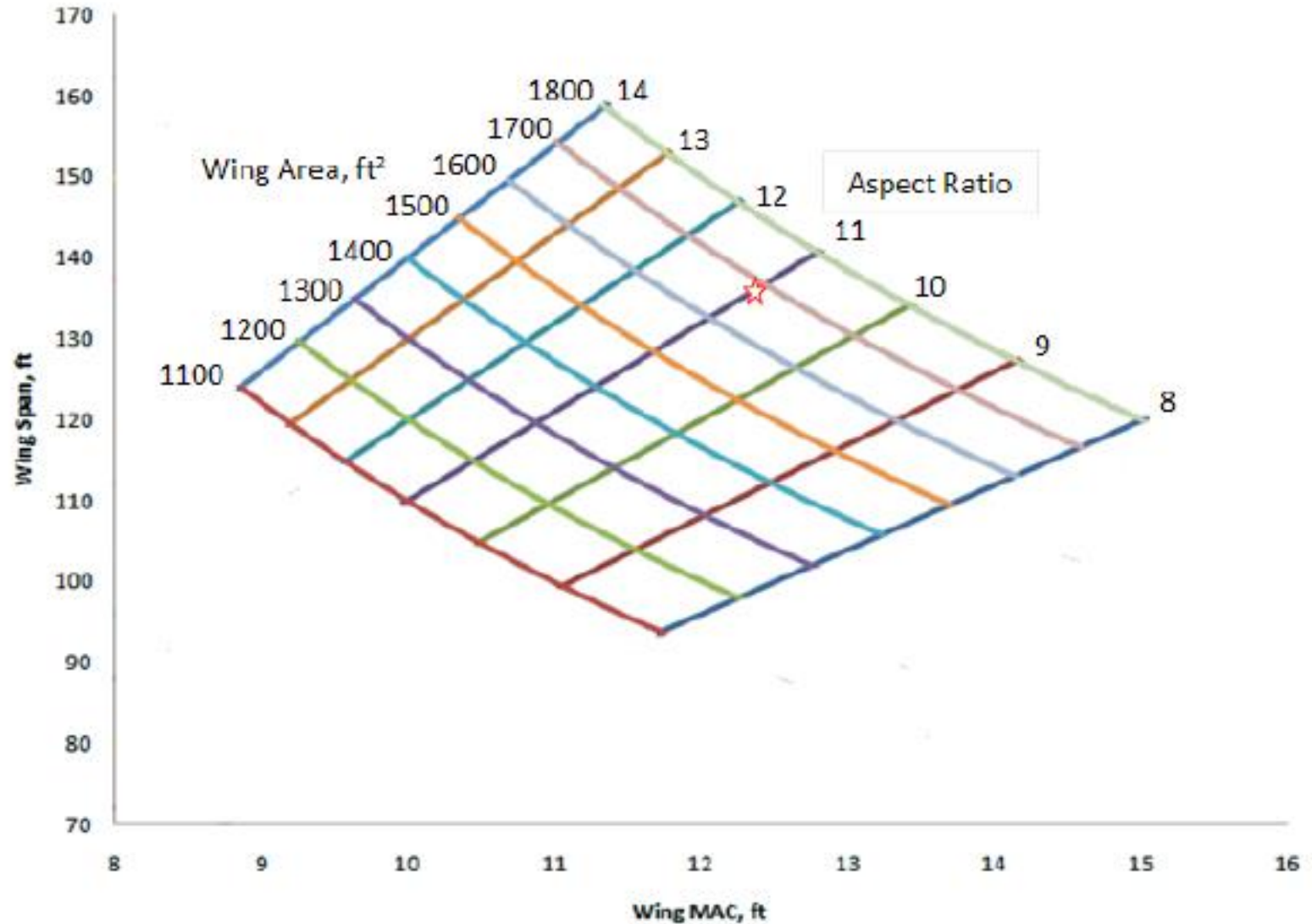
Source: 2005-06 AIAA Team Design, The Black Mamba, Cal Poly, SLO



# A Four-parameter Carpet Plot

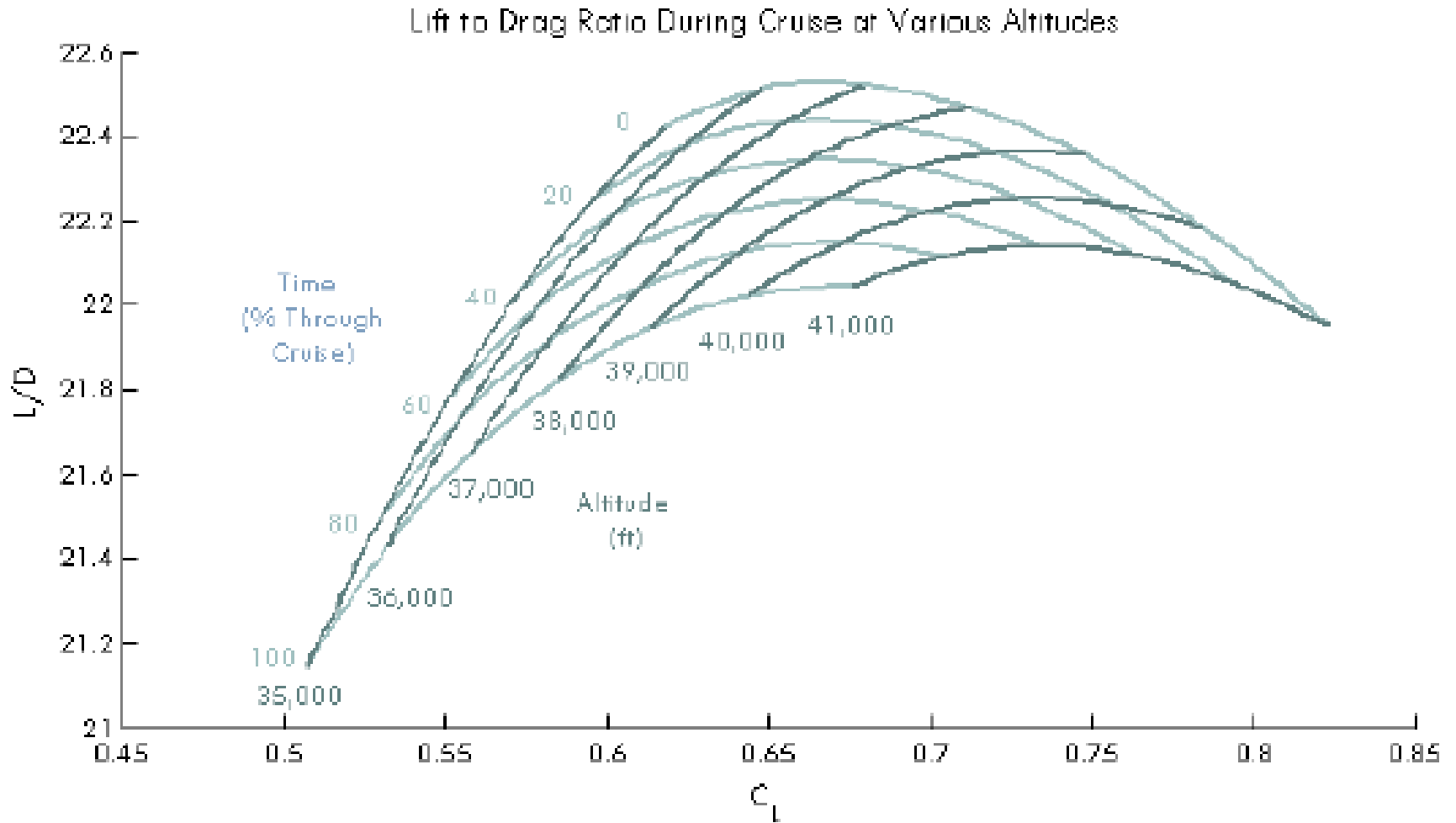


# A Four-parameter Carpet Plot





# A Four-parameter Carpet Plot



Source: 2009-10 AIAA UG Team Aircraft Design Winning Team, Cal Poly, SLO

# Recommended Readings

Ref. No.	Chapter	Author(s)	Title
AVD 1	Chapter 25	Nicolai, L.M. and Carichner, G.E.	<i>Fundamentals of Aircraft and Airship Design , Volume I—Aircraft Design ,</i> AIAA Education Series, AIAA, Reston, VA, 2010.
AVD 2	Chapter 19	Raymer, D.P.	<i>Aircraft Design : A Conceptual Approach ,</i> AIAA Education Series, AIAA, Reston, VA, 2012.
AVD 4	Chapter 20	Gudmundsson, S.	<i>General Aviation Aircraft Design: Applied Methods and Procedures ,</i> 1 <sup>st</sup> Ed., Butterworth-Heinemann, September 2013.
AVD 13	Chapter 15	Schaufele, R.D.	<i>The Elements of Aircraft Preliminary Design ,</i> Aries Publications, 2000.
AVD 21	Chapter 4	Jenkinson, L.R., and Marchman, J.F.	<i>Aircraft Design Projects for Engineering Students ,</i> Co-published by AIAA, Reston, VA, 1999

NOTE: See Appendix in Overview CM